



Electric charges & Fields

Electric charge and field

Charge → Charge is a property of object due to which it Experience or produce electromagnetic force..

Mass → quantity of matter contained in a body

$$\rho \text{ (density)} = \frac{\text{total mass}}{\text{Volume}}$$

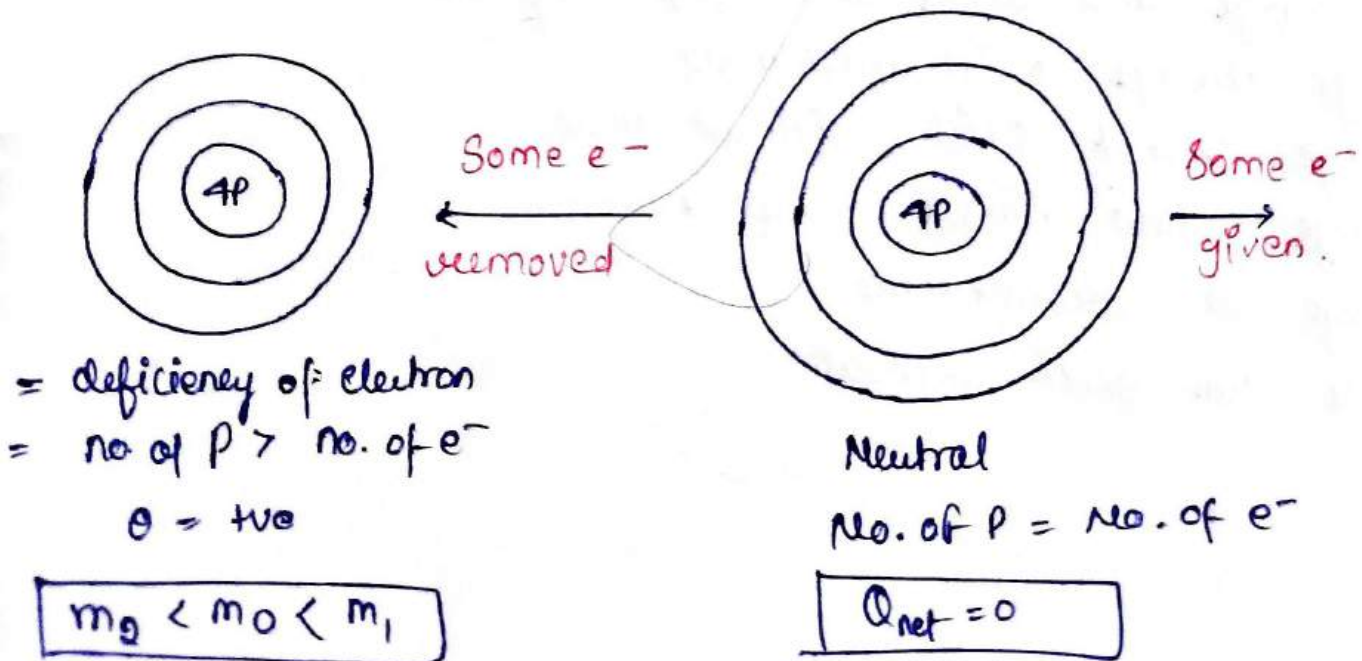
Mass → Property of object due to ~~other~~ which it attract every other matter in the Universe by gravitational force.

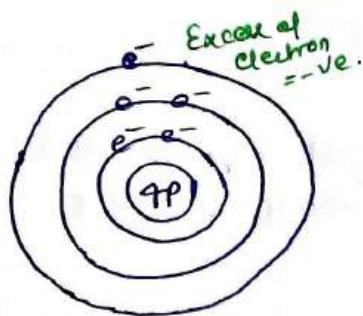
Mass → Mass is nothing but forms of energy
 $E = mc^2$

Electric field and Charge =

Charge	Electric field	Magnetic field	EM wave
Rest	✓	X	X
Const. Velocity	✓	✓	X
accelerated	✓	✓	✓

How does a body attain any charge





No. of proton < no. of e^-
 $Q = -ve$ mass - Increased.
 $m_1 > m_0$

Charge

Property of object by virtue of which it apply or experience electromagnetic force

= Scalar
 = S.I unit - Coulomb
 C.G.S unit - e.s.u (electrostatic unit)
 = 1 franklin.

$$1C = 3 \times 10^9 \text{ esu} = 3 \times 10^9$$

Practical unit - emu
 Smallest unit - e.s.u
 Largest unit - faraday

Types of charge

1. Positive charge - deficiency of e^-
2. Negative charge - Excessness of e^-

Neutral body is not a type of charge. It means uncharged body.

$$\text{no. of electrons} = \text{no. of proton.}$$

Ex! Neutron.

- ⇒ Same nature of charge
- ⇒ Same charge repel each other
- ⇒ One charge and other uncharged may attract
- ⇒ Charge always exist with mass
- ⇒ Charge cannot exist without mass
- ⇒ Charge follow simple scalar addition
- ⇒ Charge is transferable
- ⇒ Mass can exist without

Charge is Invariant

Value of charge on the body does not depend on the speed of body and also independent upon frame of reference

Q1 A positively charged body can be made neutral by
Ans giving same e^-

Q2 During charging of body mass of the body increases then body becomes

Ans Negatively charged

Q3 Smallest unit of charge
Franklin

Q4 If a body has positive charge on it, then it means it has
lost some electrons

Q5 Sure check for presence of electric charge is,

- (1) Production of Induction
- (2) Repulsion b/w bodies
- (3) Attraction b/w bodies
- (4) Frictional force b/w bodies



Charge is conserved \Rightarrow

1. Conservation of momentum
2. " " Angular momentum
3. " " Energy
4. " " Charge

Ques Charge developed

Ques find no. of e^- transferred to create 1C charge.

$$Q = ne$$
$$1\text{C} = n \times 1.6 \times 10^{-19} \text{e}$$
$$n = \frac{1}{1.6 \times 10^{-19}} = \frac{10 \times 10^{18}}{1.6} = \boxed{n = 6.25 \times 10^{18}}$$

Air is insulator upto certain limit after that it became conductor

Ques A glass rod is rubbed

$$Q = 19.2 \times 10^{-19} \text{C} = ne$$
$$19.2 \times 10^{-19} \text{C} = n \times 1.6 \times 10^{-19}$$
$$n = \frac{19.2}{1.6} = \frac{192}{16} = 12 \text{ Ans}$$

Quantization of charge

Possible charges are :-

(i) $Q = 1.6 \times 10^{-20} \text{C} = \text{Not Possible}$

(ii) $Q = 1.6 \times 10^{-20} \text{C} = \text{Possible}$

(iii) $Q = 6.4 \times 10^{-17} \text{C} = \text{Possible}$

(iv) $Q = 0.1 \text{e} = \text{Not Possible}$

(v) $Q = 0.1 \text{C} = \text{Possible}$

Specific charge

$$\sigma = \frac{q}{\text{mass}}$$

Proton =

$$\sigma = \frac{e}{m_p}$$

Deuteron = (1P + 1N) (^1_1H)

$$\sigma_0 = \frac{e}{2m_p}$$

α -particle = [^4_2He] [2P + 2N.]

$$\sigma_4 = \frac{\sigma e}{4m_p} = \frac{e}{2m_p}$$

If Speed Increase then mass increase but charge same

$$\sigma = \frac{qe}{m\uparrow} \leftarrow \text{Same}$$

σ (decrease with increase in speed)

If Speed is decreasing then specific charge will increase

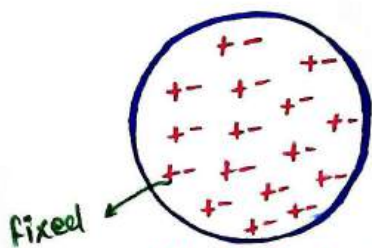
$$(\uparrow \sigma) = \frac{q}{m\downarrow}$$

CONDUCTOR \Rightarrow

Have large no. of free e^- s

(a) at Surface

(b) Inside volume of conductor



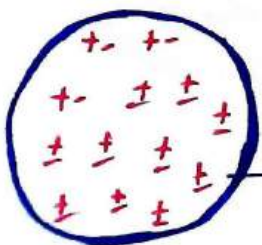
Neutral Conductor.

* Excess charge given to conductor always reside on the surface of conductor.

* Conductors allow flow of charge

Insulator \Rightarrow

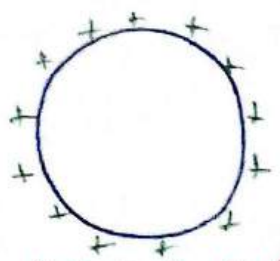
* Excess charge remains there where it is placed.



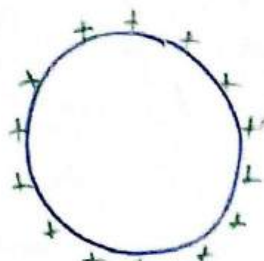
These e^- are highly & strongly bonded.

INDUCTION = Separation of charge

Excess charge



Hollow Conductor

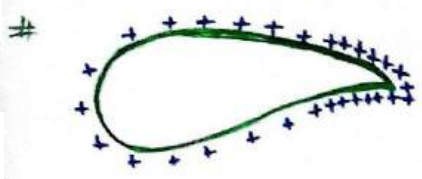


Solid Conductor



Insulator

Ex:



charge density high at sharp point.

In Conductor

In Insulator

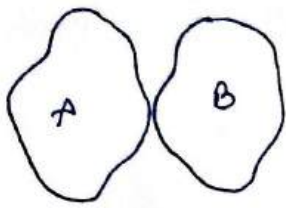
Ques If a solid and a hollow conducting sphere have same radius then.

- ① Hollow
- ② Solid
- ③
- ④

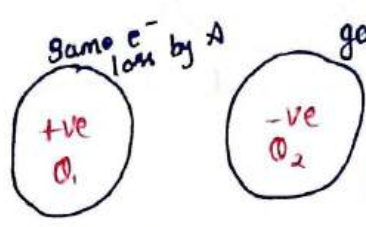
Charging of A Body

Charging by friction \Rightarrow Only few Insulators.

When two bodies are rubbed together, electrons, are transferred from one body to other making one body positively charged and the other negatively charged.



Both are neutral Insulator



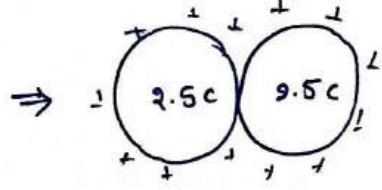
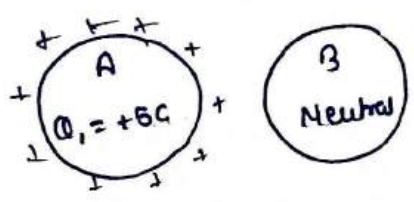
$$|Q_1| = |Q_2|$$

Same e^- loss by A
gain of some e^- by B

equal and opposite nature of charge created.

Charging by conduction \Rightarrow For Conductors.

Conduction from a charged body involve transfer of like charges. A positively charged body can cause more bodies to get positively charged. But the sum of the total charge on all positively charged bodies will be the same as charge on initial considered charged body.



a & b are touched

Ques When 10^{14} electrons

- ① 16 μ C \checkmark
- ② -16 μ C
- ③ -32 μ C
- ④ 32 μ C

$$Q = ne$$

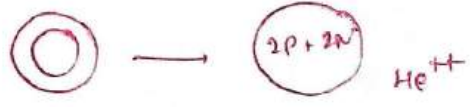
$$10^{14} \times 1.6 \times 10^{-19}$$

$$1.6 \times 10^{-5} \text{ C}$$

$$= \boxed{16 \mu\text{C}}$$

Ques Charge on α -particle is

- ① 4.8×10^{-19}
- ② $3.2 \times 10^{-19} \text{ C}$
- ③ $1.6 \times 10^{-19} \text{ C}$
- ④ $6.4 \times 10^{-19} \text{ C}$



Q1 A body has -80 micro coulomb of charge

- ① 8×10^{-5}
- ② 80×10^{-17}
- ③ 8×10^{14}
- ④ 1.28×10^{-14}

$$Q = ne$$

$$-80 \times 10^{-6} = +n \times 1.6 \times 10^{-19}$$

$$60 \times 10^{-6} \times 10^{19} = n$$

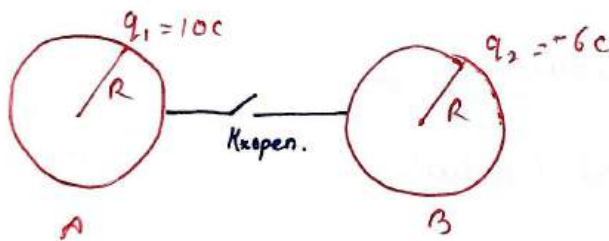
$$\boxed{50 \times 10^{13} = n}$$

+ve = deficiency e^-

Q2 A conductor has

- ① 9 electron in excess
- ② 27 electron in short
- ③
- ④

Q3 Find charge



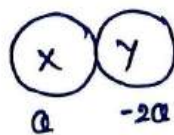
$$q_{1 \text{ final}} = \left(\frac{R}{R_1 + R_2} \right) (10 - 6) = \frac{1}{2} \times 4 = 2C$$

$$q_{2 \text{ final}} = +2C$$

Q4 When three identical spheres X, Y and Z having charge q , $-2q$ and $3q$ respectively, At first X and Y are in contact then Y and Z are in contact then final charge on X, Y and Z will be.

- ① $\frac{q}{2}, \frac{3q}{2}, \frac{q}{2}$
- ② $\frac{-q}{2}, \frac{5q}{4}, \frac{+5q}{4}$
- ③ q, q, q
- ④ $\frac{q}{2}, \frac{3q}{2}, \frac{-q}{2}$

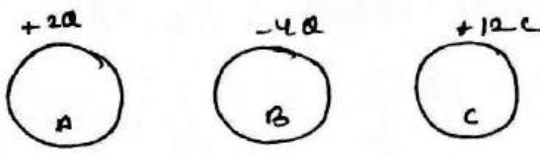
X & Y in contact



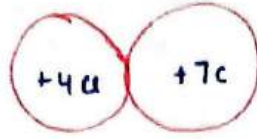
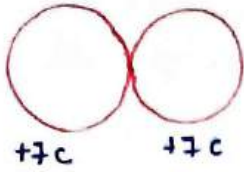
$$q_x = -\frac{q}{2} \quad q_y = -\frac{q}{2}$$

$$q_y = \frac{5q}{4} = q_z$$

Ques



1st A & C are touched then
B & C are touched then find
charge on each sphere

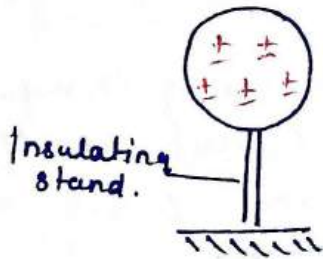


$$Q_B = Q_C = \frac{8q}{2}$$

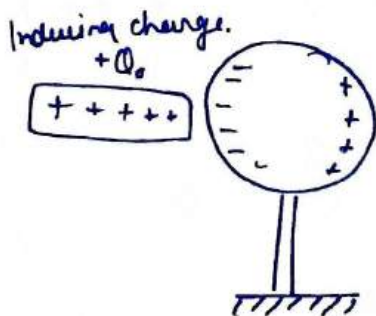
Charging by Induction \Rightarrow

A body can be charged by induction \Rightarrow

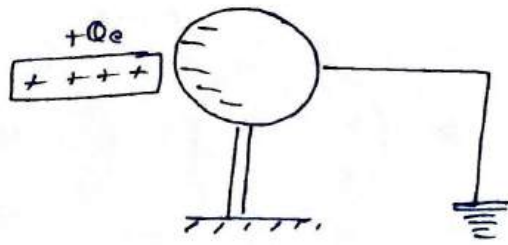
Step-1 Take an isolated neutral conductor.



Step-2 Take a positively or negatively charged rod near to sphere



Step-3 Now earthing the sphere.

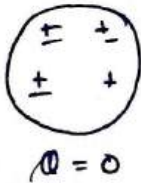


Step-4 Removing earthing & Rod.

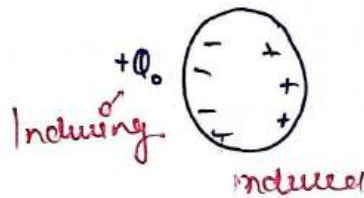


* 2nd method of Inducting

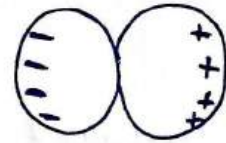
Step-1 = take a Neutral sphere



Step-2 = Placed +Q₀ charge near to sphere



Step-3 Now take identical Neutral sphere & placed in contact with this sphere



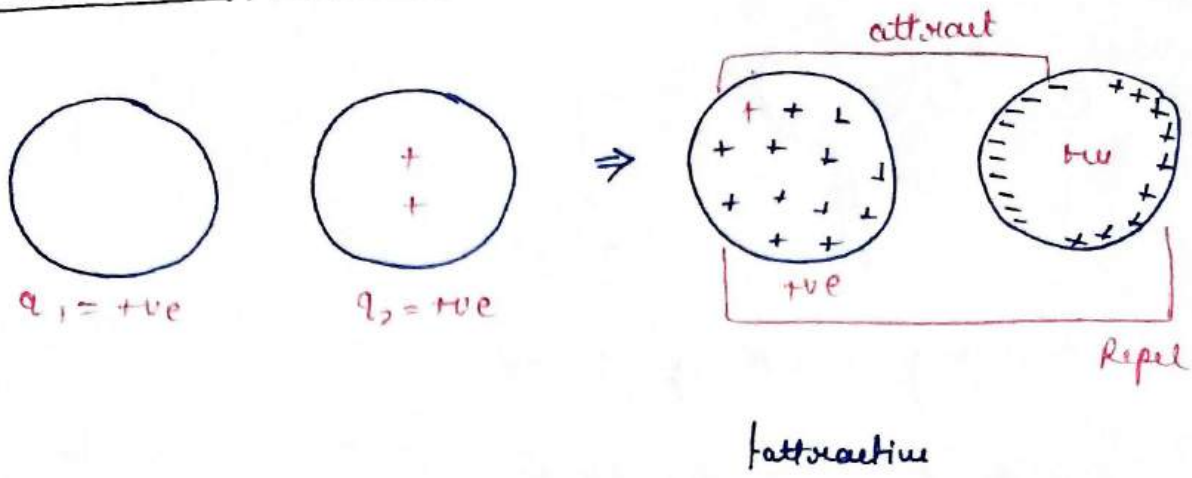
Step-4 Remove 2nd Sphere & +Q₀ charge



$$Q_{\text{Induced}} = -Q_{\text{Inducing}} \text{ (For Conductor)}$$

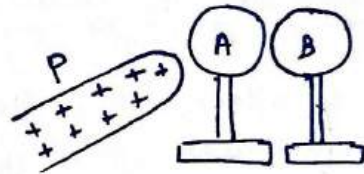
$$Q_{\text{Induce}} \leq Q_{\text{Inducing charge}}$$

Attraction force b/w same nature of charge body



Ques Two uncharged metal sphere placed in contact as shown in figure and a positive charged rod placed in contact with A, then charge on A and B will be

- ① Both became +ve ✓
- ② Both became -ve
- ③ A -ve and B became +ve
- ④ A became +ve and -ve



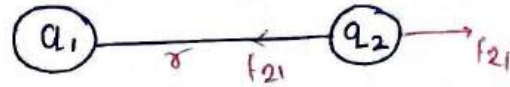
Ans Two Uncharged

Ans In induction the charge induced

Coulomb's law \Rightarrow

$$|\vec{F}_{12}| = |\vec{F}_{21}|$$

action reaction pair



Electrostatic \rightarrow

- Central force / always along line joining.
- Conservative
- long range / infinite
- follow - Inverse square law
- depends on medium
- conservative in nature
- may be attractive or repulsive
- mediated by photon.

* gravitational force always attractive

$$|\vec{F}_{21}| \propto \frac{q_1 q_2}{r^2}$$

$$|\vec{F}_{21}| = \frac{k q_1 q_2}{r^2} = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r^2}$$

$\epsilon_0 =$ permittivity of free space

Property of medium which define electric field line

$$|\vec{F}_{21}| = |\vec{F}_{12}| = \frac{q_1 q_2}{4\pi\epsilon_0 r^2}$$

$$k = \left(\frac{1}{4\pi\epsilon_0}\right) = 9 \times 10^9 \text{ Nm}^2/\text{C}^2$$

in free space

$$|\vec{F}_{21}| = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2}{r^2}$$

force on 2nd charge due to 1st charge

Net electrostatic on 2nd charge

$$\epsilon_0 = 8.85 \times 10^{-12} \text{ C}^2/\text{Nm}^2$$

other medium (ϵ_{r0})

$$|\vec{F}_{21}| = \frac{1}{4\pi\epsilon_{r0}} \frac{q_1 q_2}{r^2}$$

force on 2nd charge due to 1st charge

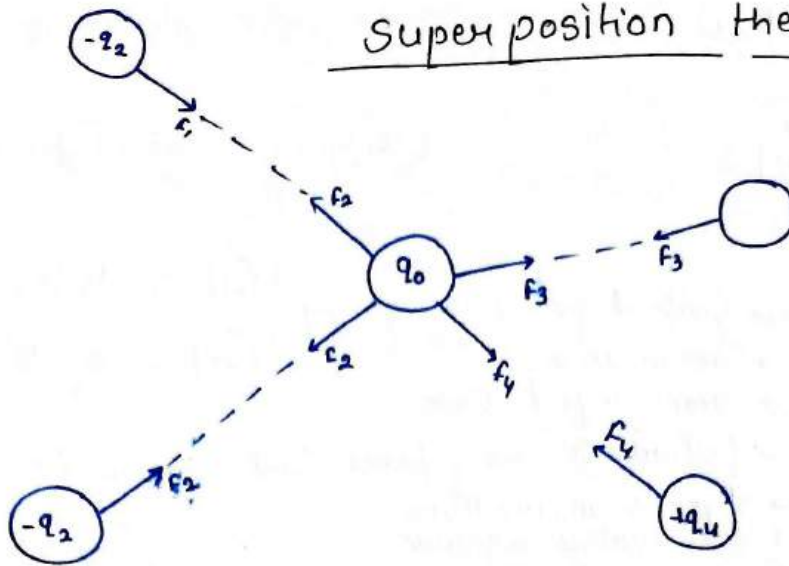
other medium (ϵ_m)

$$\vec{F}_{(2^{nd})} = \frac{q_1 q_2}{4\pi\epsilon_m r^2}$$

Net electrostatic force on 2nd charge

- (A) Electrostatic force depend on medium
- (B) Electrostatic force on one charge due to other does not depend on medium.
- ① Both are true ✓
- ② Both are false
- ③ A - T, B - false
- ④ A - F - B - T

Superposition theorem



$$\# \vec{F}_{\text{net on } q_0} = \vec{F}_1 + \vec{F}_2 + \vec{F}_3 + \vec{F}_4 \text{ ---}$$

Force b/w any two charges does not depend on presence of other charge and medium.

Relative permittivity / dielectric constant =

$$k = \epsilon_r = \frac{\epsilon_m}{\epsilon_0}$$

↳ Unit less
dimensionless

$$\epsilon_m = \epsilon_r \epsilon_0$$

$$\epsilon_m = \epsilon_r \epsilon_0 = k \epsilon_0$$

$$f_0 = \frac{q_1 q_2}{4\pi \epsilon_0 r^2}$$

$$f_m = \frac{q_1 q_2}{4\pi \epsilon_m r^2} = \frac{q_1 q_2}{4\pi \epsilon_0 r^2 k} = \frac{f_0}{k} = \frac{f_0}{\epsilon_r}$$

Q11 Two charge of 1 nC

$$F = \frac{k q_1 q_2}{r^2} = \frac{9 \times 10^9 \times 1 \times 10^{-9} \times 1 \times 10^{-9}}{(3 \times 10^{-2})^2}$$

$$\frac{9 \times 10^{-9}}{9 \times 10^{-4}} = \frac{10^{-5}}{10^{-4}} \text{ N} = \boxed{10 \mu\text{N}}$$

Ques Charge 3 esu and 12 esu is placed at 3cm then find electrostatic force.

$$1c = 3 \times 10^9 \text{ es.u}$$

$$q_1 = 3 \text{ esu} = 3 \times \frac{1c}{3 \times 10^9} = 10^{-9} \text{ C}$$

$$q_2 = 12 \text{ esu} = \frac{1}{3 \times 10^9} \times 12^4 = 4 \times 10^{-9} \text{ C}$$

$$F_{12} = \frac{9 \times 10^8 \times 10^{-9} \times 4 \times 10^{-9}}{(3 \times 10^{-2})^2}$$

$$= 4 \times 10^{-5} \text{ N}$$

$$\boxed{4 \text{ dyne}}$$

Ques Two charge q_1 & q_2 apply force on each other f_0 when in air find force applied on each other when placed in a medium of dielectric constant ϵ_1 . also find net force on charge q_1 in medium.

Solⁿ ① $f_m = \frac{f_0}{\epsilon_1}$

② $f_m = f_0$ ✓

③ $f_m = \epsilon_1 f_0$

Ques f_g and f_e represent

① 10^{42} ✓

② 10

③ 1

④ 10^{-4}

$$\frac{f_g = \frac{Gm^2}{r^2}}{f_e = \frac{ke^2}{r^2}}$$

$$= \frac{6.6 \times 10^{-11} \times 10^{-60}}{9 \times 10^9 \times (1.6 \times 10^{-19})^2} = \frac{10^{-80}}{10^{-38}} = 10^{-42}$$

Ques



$$F = \left(\frac{k q_1 q_2}{r^2} \right) = 64 \text{ N}$$

$$F' = \frac{k q_1 q_2}{(4r)^2} = \frac{4 k q_1 q_2}{16 r^2}$$

$$= \frac{64}{4} = \boxed{16 \text{ N}}$$

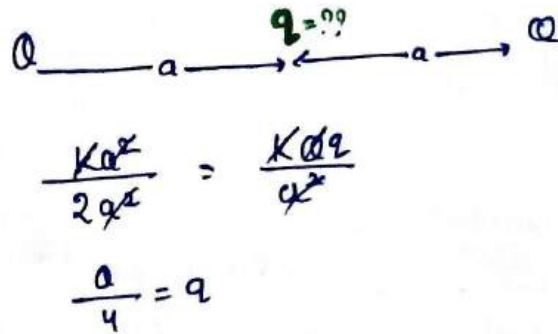
$$F \propto \frac{q_1 q_2}{r^2} =$$

Ques Charges Q, q

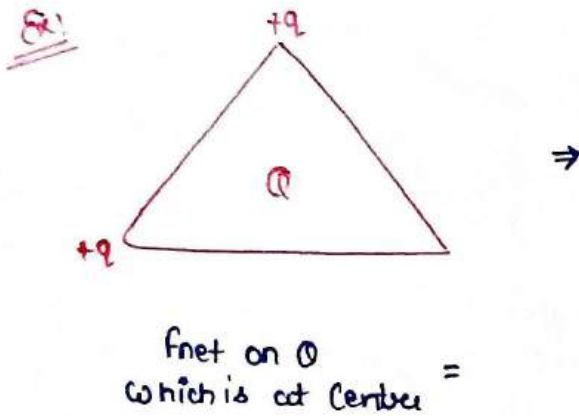
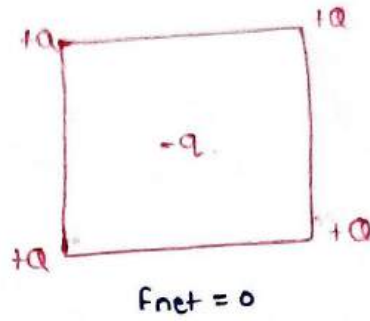
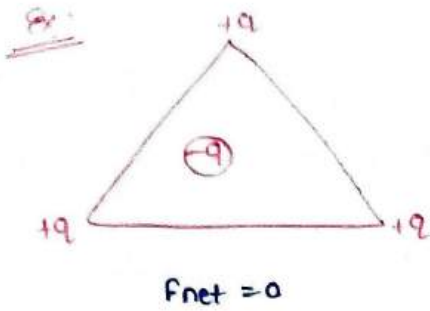
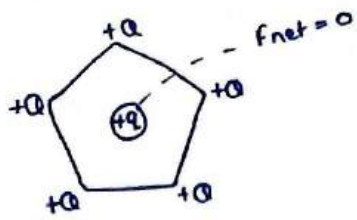
- ① q
- ② $Q/2$
- ③ $-Q/2$
- ④ $-Q$

Ques A charge q is

- ① $Q/4$
- ② $-Q/4$ ✓
- ③ Q
- ④ $-Q/8$



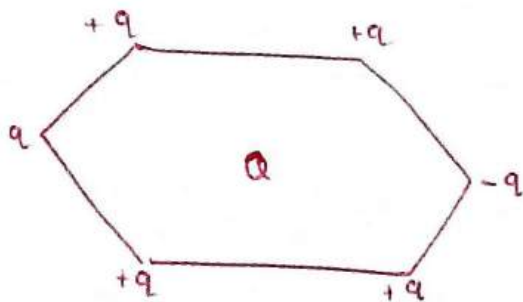
Ques Two small conducting



Ques Five point charges, each of value $+q$, are placed on five vertices of a regular

- ① $\frac{1}{\pi \epsilon_0} \left(\frac{q}{L}\right)^2$
- ② $\frac{2}{\pi \epsilon_0} \left(\frac{q}{L}\right)^2$
- ③ $\frac{1}{2\pi \epsilon_0} \left(\frac{q}{L}\right)^2$
- ④ $\frac{1}{4\pi \epsilon_0} \left(\frac{q}{L}\right)^2$ ✓✓

Q Find net force on charge Q which is at centre



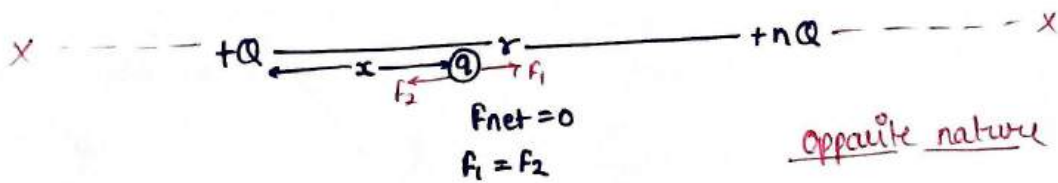
Q. Find position of 3rd charge so that force on 3rd charge will zero



Q1 Two charge Q_1 and Q_2 shows repulsion then which of the following option is correct for this.

- ① $Q_1 \times Q_2 = 0$
- ② $Q_1 \times Q_2 > 0$ ✓
- ③ $Q_1 \times Q_2 < 0$
- ④ all of these

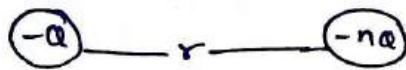
Q2 Find position of 3rd charge q in given system so that net force experienced by q is zero.



From small charge. $x = \frac{r}{\sqrt{x+1}}$



$$x = \frac{r}{\sqrt{x-1}}$$



Q3 Find position and value of 3rd charge so that complete system will be in equilibrium.



Step-1

1. Find position of 3rd charge so that 3rd charge in equilibrium.

2. Find nature of third charge.

3. Find value of 'q' so that force on any other two charge is zero

net on +Q is zero

$$\frac{kQ^2}{\left(\frac{r}{\sqrt{x+1}}\right)^2} = \frac{knaq}{r^2}$$

$$q(\sqrt{x+1})^2 = na$$

$$q = \frac{na}{(\sqrt{x+1})^2} \quad R$$

$$q = \frac{na}{(\sqrt{n-1})^2}$$

for opposite nature of initial two charge

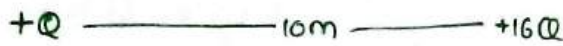
Q find distance from $9Q$ where charge is placed to experience zero force.



$$x = \frac{18}{\sqrt{9}-1} = \frac{18}{3-1} = \frac{18}{2} = 9\text{m}$$

from $9Q$ dist = $18 + 9 = 27\text{m}$

Q find the value and position of q so that system will be in equilibrium.

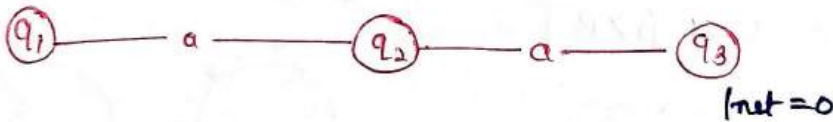


$$x = \frac{10}{\sqrt{16}+1} = \frac{10}{5} = 2\text{m from } +Q \text{ and } 10-2 = 8\text{m from } 16Q.$$

• Q ka nature = -ve

$$q = \frac{16Q}{(\sqrt{16}+1)^2} = \frac{-16Q}{25}$$

Q If net force of q_3 is zero then find relation b/w q_1 and q_2



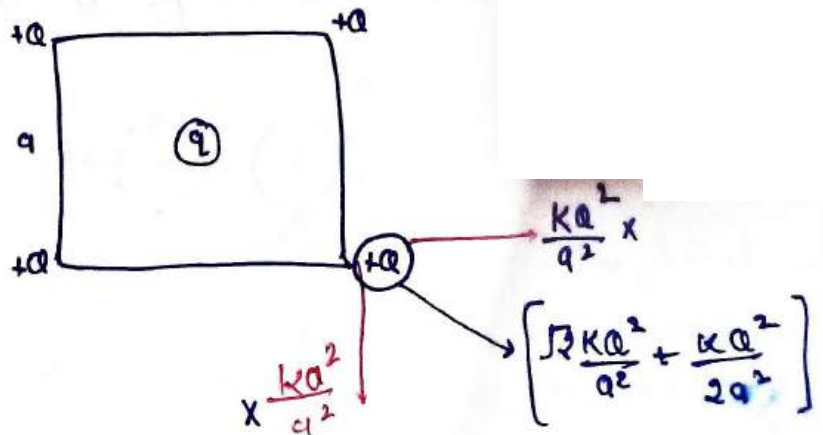
$$\frac{kq_1q_3}{(2a)^2} = \frac{kq_2q_3}{a^2} \Rightarrow \frac{q_1}{4} = q_2$$

$$\boxed{q_1 = -4q_2}$$

Q find value of q so that system is in equilibrium.

Net force on q placed at centre = 0

q must be = -ve



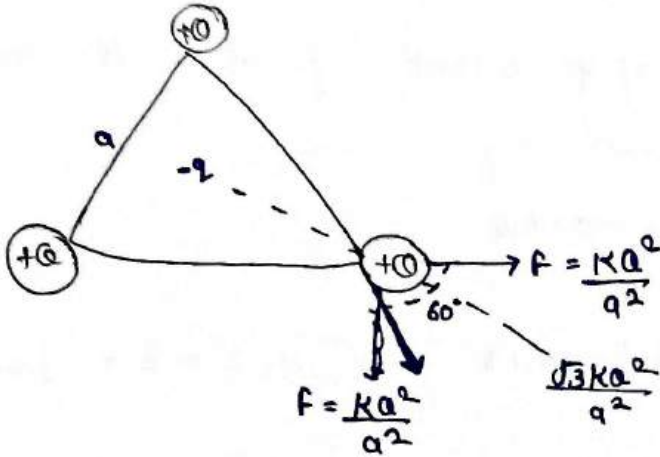
$$\frac{KqQ}{\left(\frac{a}{\sqrt{2}}\right)^2} = \frac{Ka^2}{a^2} \left[\sqrt{2} + \frac{1}{2} \right]$$

$$2q = a \left[\frac{2\sqrt{2}+1}{2} \right]$$

$$q = \frac{a}{4} (2\sqrt{2}+1)$$

$$q = -\frac{Q}{4} (2\sqrt{2}+1) \quad \underline{\underline{A_1}}$$

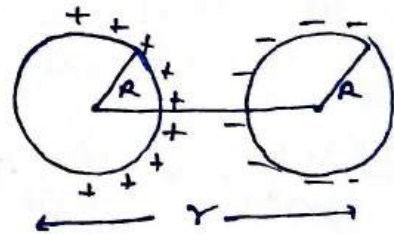
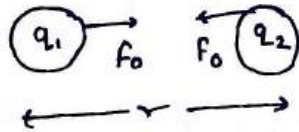
Ques



$$\frac{3KqQ}{a^2} = \sqrt{3} KQ^2$$

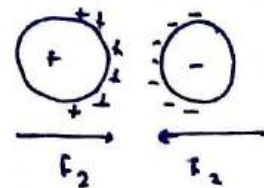
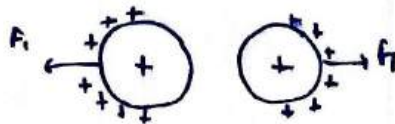
Ques electrostatic attraction b/w two point charge is f_0 . when they are placed at x . if they are given to the conducting sphere of radius R . then electrostatic attraction will be. if distance b/w centre of sphere is x ($x > R$)

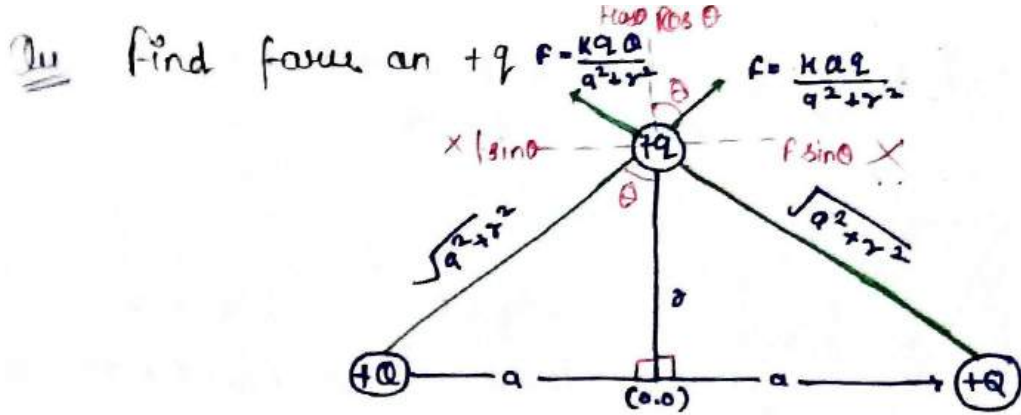
- ① $F > f_0$ ✓
- ② $F < f_0$
- ③ $F = f_0$
- ④ zero



Ques Two identical sphere are given equal charge in one case & opposite charge in another case having force f_1 & f_2 respectively distance b/w sphere is not large as compare to diameter then compare f_1 & f_2 .

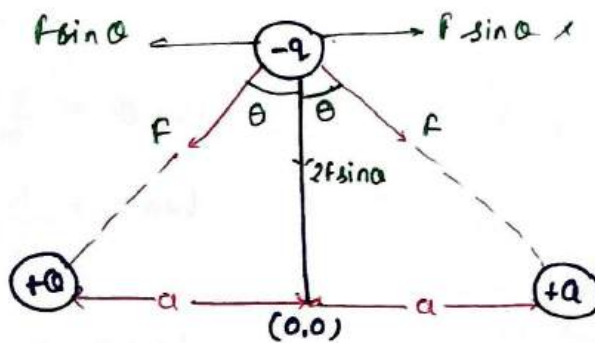
- ① $f_1 > f_2$
- ② $f_1 = f_2$
- ③ $f_1 < f_2$ ✓✓
- ④ Information is not sufficient to draw the conclusion.





$$F_{net} = 2F \cos \theta$$

$$2 \frac{kQq}{(a^2+r^2)^2} \times \frac{r}{\sqrt{a^2+r^2}} = \boxed{F_{net} = \frac{2kQqr}{(a^2+r^2)^{3/2}}}$$



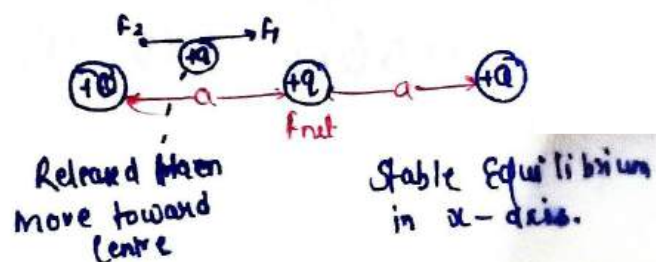
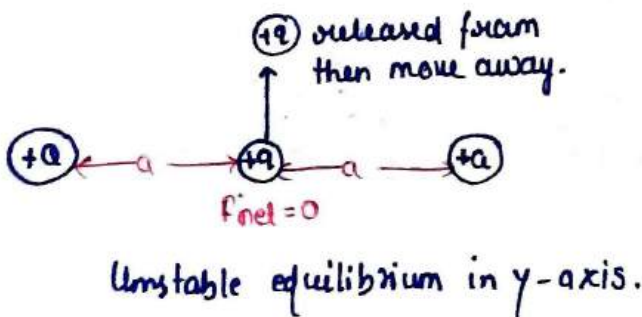
$$\boxed{F_{net} = \frac{2kQqr}{(a^2+r^2)^{3/2}}}$$

Unstable Equilibrium

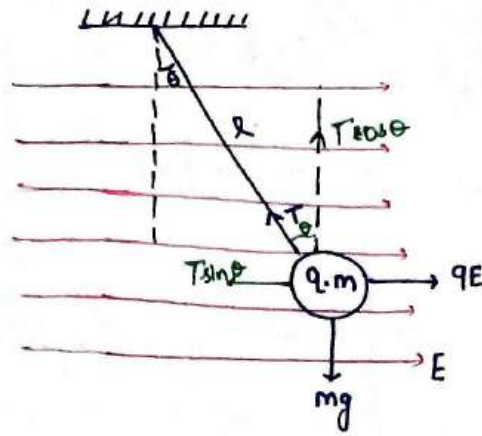
Stable Equilibrium



Ex:



Pendulum problem \Rightarrow Force on q charge in electric field is $F = qE$



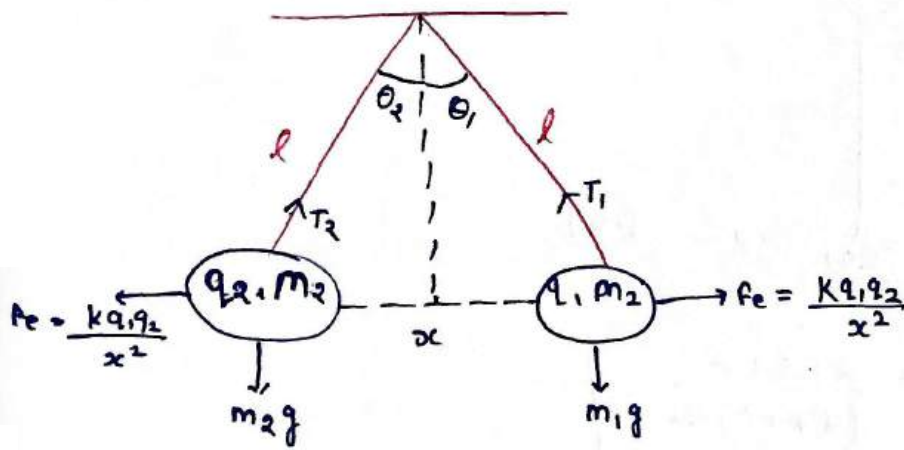
$$E_f y = 0 \quad E_f x = 0$$

$$T \cos \theta = mg \quad \text{--- (i)} \quad T \sin \theta = qE \quad \text{--- (ii)}$$

(i) / (ii)

$$\frac{T \sin \theta}{T \cos \theta} = \frac{qE}{mg}$$

$$\boxed{\tan \theta = \frac{qE}{mg}}$$



$$\tan \theta = \frac{qE}{mg}$$

$$\tan \theta_1 = \frac{kq_1q_2}{x^2 m_1 g} \quad \text{--- (i)}$$

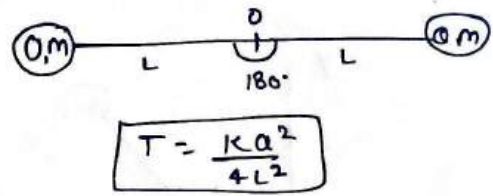
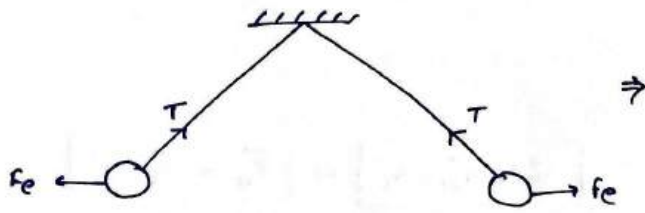
$$\tan \theta_2 = \frac{kq_1q_2}{x^2 m_2 g} \quad \text{--- (ii)}$$

$$\frac{(i)}{(ii)} \Rightarrow \boxed{\frac{\tan \theta_1}{\tan \theta_2} = \frac{m_2}{m_1}}$$

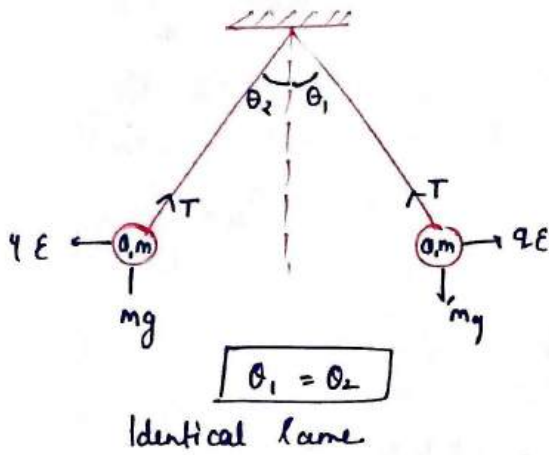
Ratio of θ_1 & θ_2 does not depend on charges q_1 & q_2 .

Ques

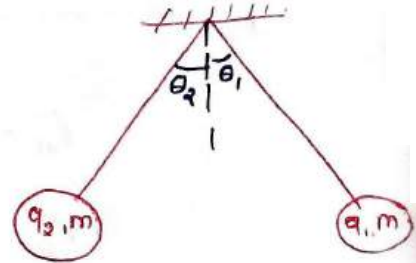
- (1) $180^\circ, \frac{1}{4\pi\epsilon_0} \frac{Q^2}{(2L)^2}$ (2) $90^\circ, \frac{1}{4\pi\epsilon_0} \frac{Q^2}{L^2}$



Ques



Ques



If $q_1 > q_2$

$m_1 = m_2 = m$

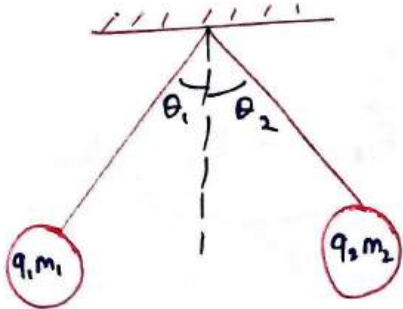
- ① $\theta_1 > \theta_2$ ② $\theta_1 < \theta_2$ ③ $\theta_1 = \theta_2$ ✓

$$\tan \theta_1 = \frac{q_1 q_2}{\cancel{q_1} m_1 g}$$

$$\tan \theta_2 = \frac{q_1 q_2}{\cancel{q_2} m_2 g}$$

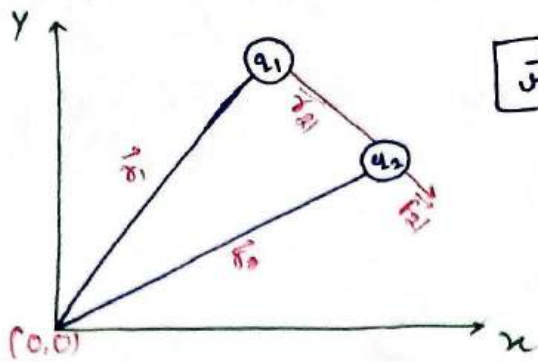
$\tan \theta_1 = \tan \theta_2$

Ques



If $q_1 > q_2$ but $m_1 < m_2$ then correct

- ① $\theta_1 = \theta_2$ ② $\theta_1 > \theta_2$ ③ $\theta_1 < \theta_2$



$$\vec{r}_1 + \vec{r}_{21} = \vec{r}_2 \quad \text{or} \quad \vec{r}_{21} = \vec{r}_2 - \vec{r}_1$$

Position of 2nd charge w.r.t 1st charge

$$\hat{r}_{21} = \frac{\vec{r}_{21}}{|\vec{r}_{21}|}$$

$$\hat{r}_{21} = \frac{\vec{r}_2 - \vec{r}_1}{|\vec{r}_2 - \vec{r}_1|}$$

$$\vec{F}_{21} = \frac{k q_1 q_2}{|\vec{r}_{21}|^2} \hat{r}_{21}$$

$$\vec{F}_{21} = \frac{k q_1 q_2}{|\vec{r}_{21}|^2} \times \vec{r}_{21}$$

$$\vec{F}_{21} = \frac{k q_1 q_2}{|\vec{r}_{21}|^2} \hat{r}_{21} = \frac{k q_1 q_2}{|\vec{r}_{21}|^3} \times \vec{r}_{21}$$

Put charge with sign.

$$\vec{F}_{21} = \frac{k q_1 q_2}{|\vec{r}_{21}|^3} \vec{r}_{21} = \frac{k q_1 q_2}{|\vec{r}_{21}|^2} \hat{r}_{21}$$

$$\vec{F}_{12} = \frac{k q_1 q_2}{|\vec{r}_{12}|^2} \hat{r}_{12}$$

$$\vec{F}_{12} = -\vec{F}_{21} \quad \text{Action reaction pair.}$$

Ques Find force applied by 2C charge

$$\begin{array}{ccc} 2C & \longrightarrow & 5C \\ (2, 3, 4) & & (5, 7, 9) \end{array}$$

$$\vec{r}_{21} = \vec{r}_2 - \vec{r}_1$$

$$= 5\hat{i} + 7\hat{j} + 9\hat{k} - 2\hat{i} - 3\hat{j} - 4\hat{k}$$

$$\vec{r}_{21} = 3\hat{i} + 4\hat{j} + 5\hat{k}$$

$$\vec{F}_{21} = \frac{k 2C \times 5C}{|\vec{r}_{21}|^3} \times \vec{r}_{21}$$

$$\frac{10k [3\hat{i} + 4\hat{j} + 5\hat{k}]}{(\sqrt{3^2 + 4^2 + 5^2})^3}$$

$$\frac{10k [3\hat{i} + 4\hat{j} + 5\hat{k}]}{(50)^{3/2}}$$

Electric field = electrostatic force experienced by 1C charge.



Electrostatic (F) force = $\frac{kQ_1 Q_2}{r^2}$

$F = \frac{kQ_1 1C}{r^2} = \underline{\underline{\text{Electric field}}}$

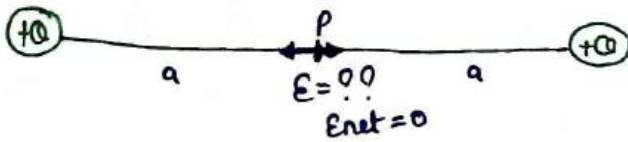
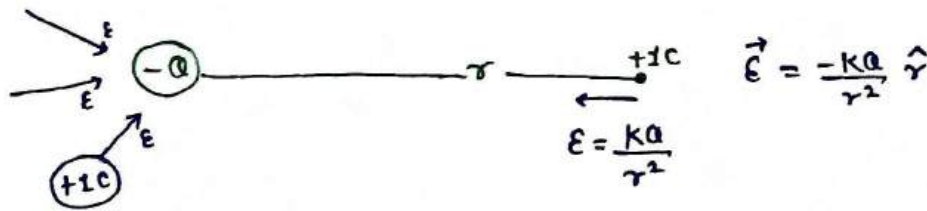
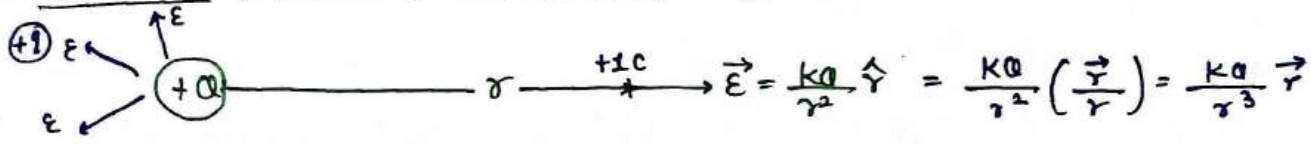
Force experienced by 1C = E
Force on qc is = qE

$\vec{F} = q\vec{E}$

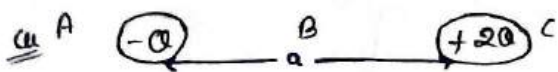
$\vec{F} = -q\vec{E}$

- force on +ve charge along electric field
- force on -ve charge opposite to electric field.

* Electric field in Vector form ✨



(one charge) $E = \frac{kQ}{a^2}$



In which region electric field will be zero.

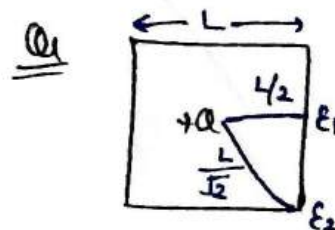
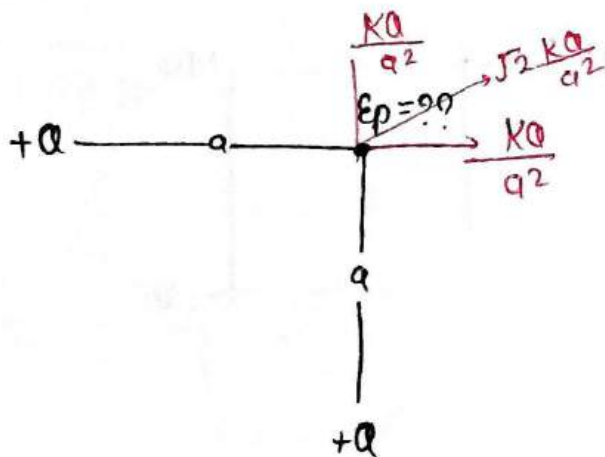
Q2 Find total net force

Q3 Find electric field at origin.

(0,0) +q

$$E_{net} = kq \left(1 - \frac{1}{4} + \frac{1}{16} - \frac{1}{64} + \dots \right)$$

$$kq \left[\frac{1}{1 - (-\frac{1}{4})} \right] \Rightarrow kq \left[\frac{1}{\frac{4+1}{4}} \right] = \frac{4kq}{5} \hat{u}_x$$



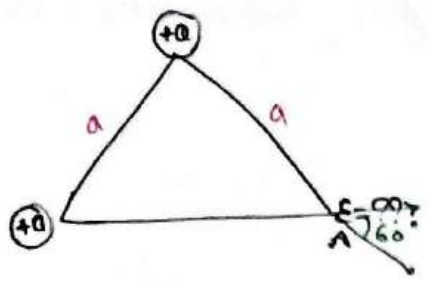
Find $\frac{E_1}{E_2} = ?$

$$E_1 = \frac{kQ}{\left(\frac{L}{2}\right)^2} = \frac{4kQ}{L^2}$$

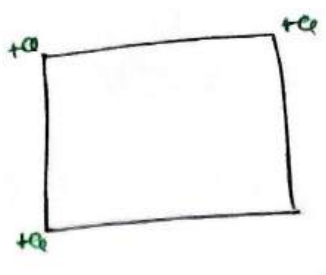
$$E_2 = \frac{kQ}{\left(\frac{L}{\sqrt{2}}\right)^2} = \frac{2kQ}{L^2}$$

$$\boxed{\frac{E_1}{E_2} = 2:1}$$

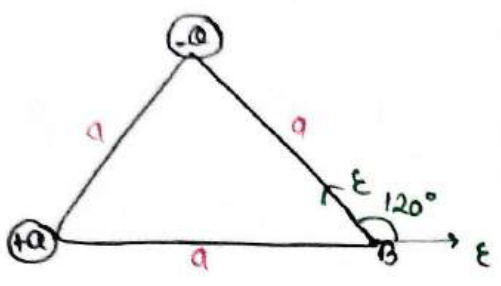
Q11



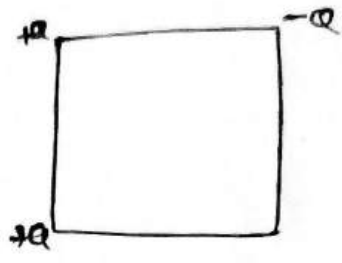
Q12



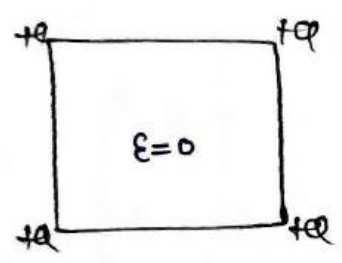
Q13



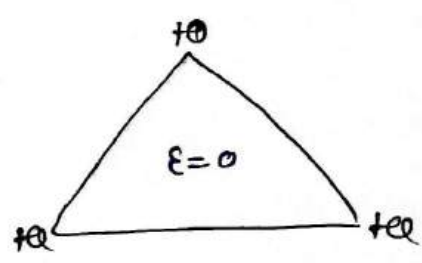
Q14



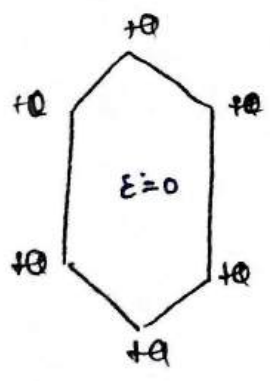
Q15



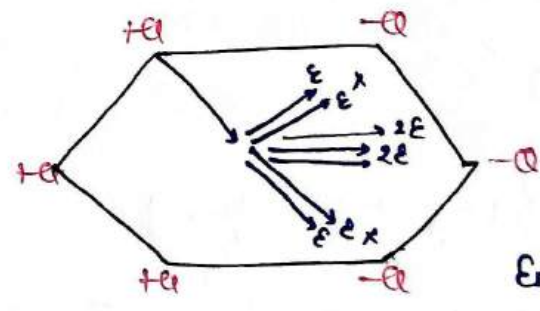
Q16



Q17



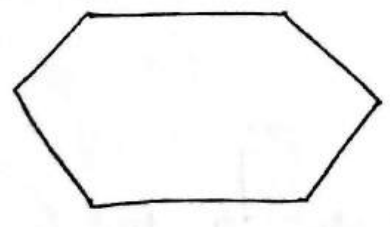
Q18



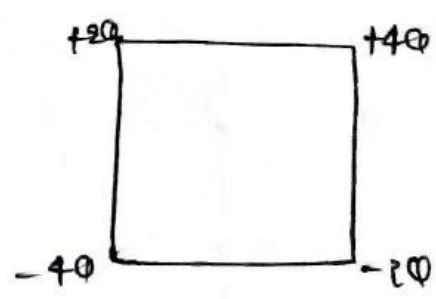
$E_{net} = 4E$

$E = \frac{kq}{L^2}$

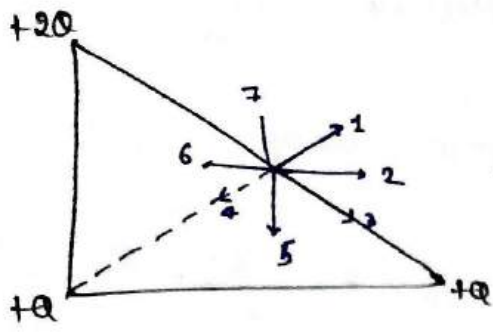
$\frac{4kq}{L^2} = \left(\frac{Q}{4\pi\epsilon_0 L^2} \right) k$



Q19



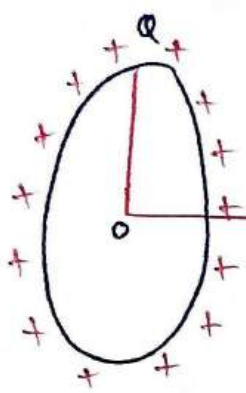
Ques



Ans 2



Electric field due to ring



$$E = \frac{kQx}{(R^2+x^2)^{3/2}}$$

$E_0 = 0$
at $x = 0$
centre

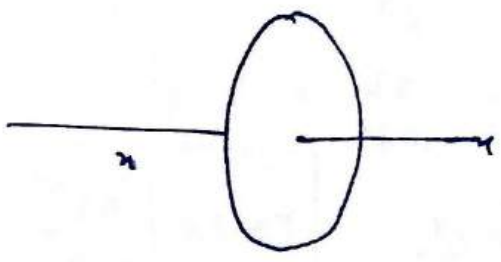
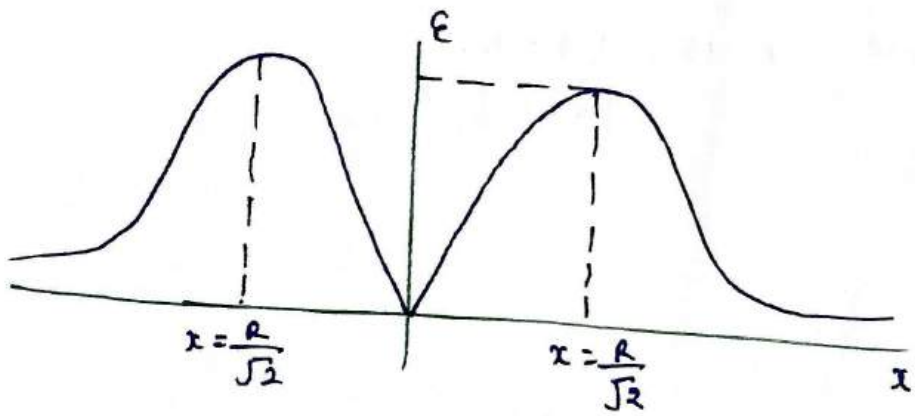
IF $x \ll R$

$$E = \frac{kQx}{R^3}$$

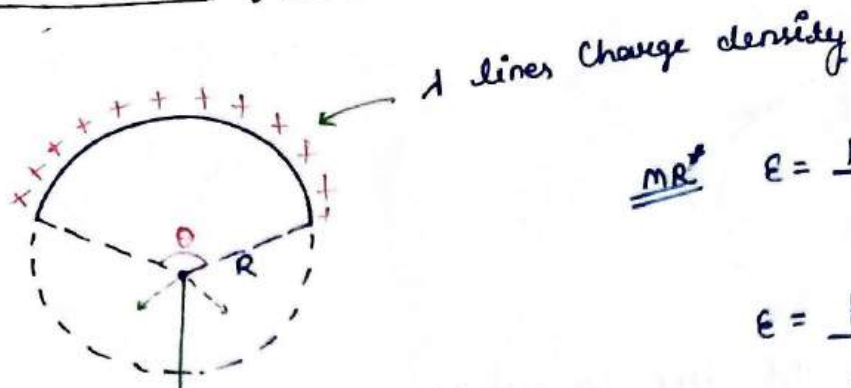
IF $x \gg R$

$$E = \frac{kQx}{x^3} = \frac{kQ}{x^2}$$

line point charge



Electric field due to Circular disk



lambda lines charge density

$$\underline{MR^2} \quad E = \frac{kq}{R^2} \cdot \frac{\sin(\theta/2)}{(\theta/2)}$$

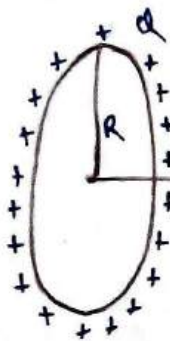
$$E = \frac{k \lambda R \theta \sin(\theta/2)}{R^2 (\theta/2)}$$

$$\boxed{E = \frac{2k\lambda}{R} \sin\left(\frac{\theta}{2}\right)}$$

$$\therefore \lambda = \frac{q}{R\theta}$$

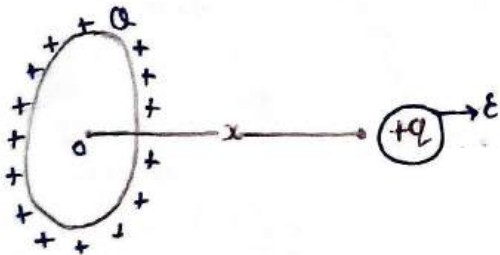
$$q = \lambda R\theta$$

$$E = \frac{2k\lambda}{R} \sin\left(\frac{\theta}{2}\right)$$

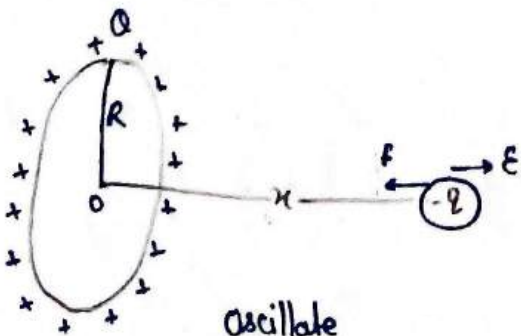


$$E = \frac{kQx}{(R^2+x^2)^{3/2}}$$

Force on ring due to +q charge



$$F = qE = \frac{kQxq}{(R^2+x^2)^{3/2}}$$



Oscillate

$$ma = \frac{kQqx}{R^3}$$

$$a = \frac{kQq}{mR^2} x$$

$$F = \frac{kQqx}{(R^2+x^2)^{3/2}}$$

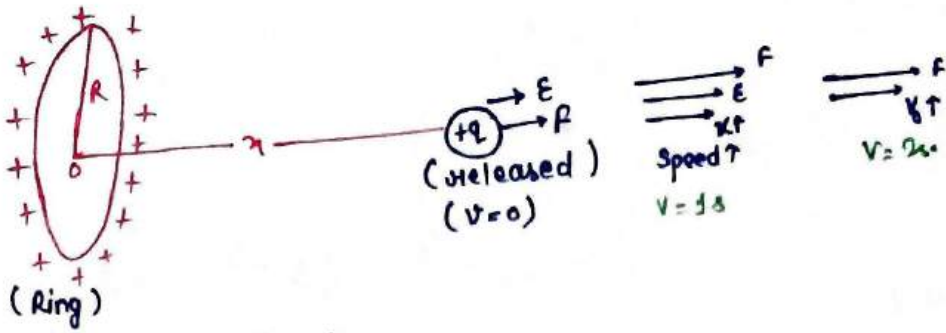
S.H.M ($x \ll R$)

$$\# \quad \omega = \sqrt{\frac{kQq}{mR^3}}$$

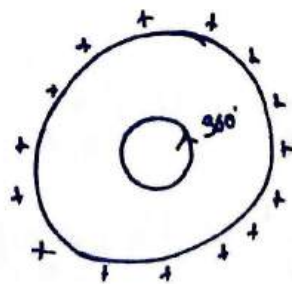
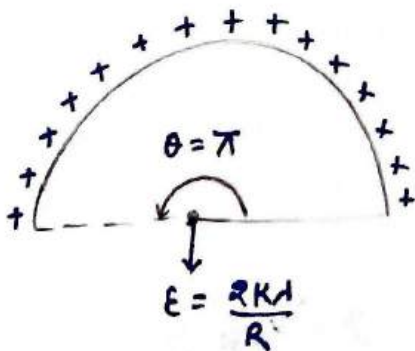
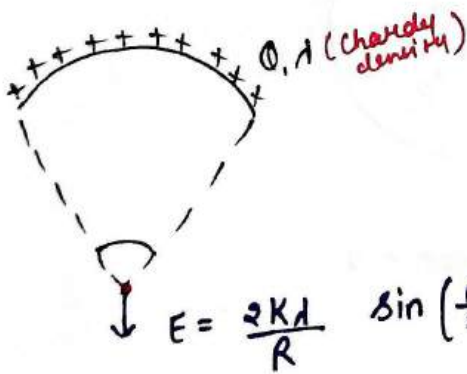
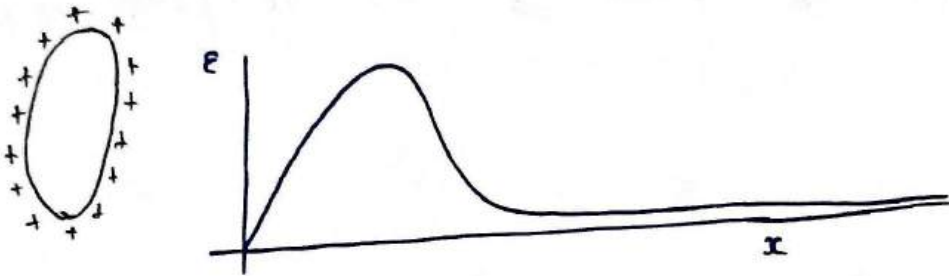
$$\boxed{T = 2\pi \sqrt{\frac{mR^3}{kQq}}}$$

Time Period oscillation.

Q.1

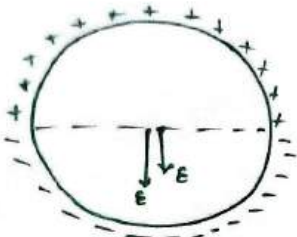


- (a) charge will oscillate
- (b) moving away & speed increasing
- (c) moving away & speed decreasing
- (d) moving away & speed \uparrow then decreasing



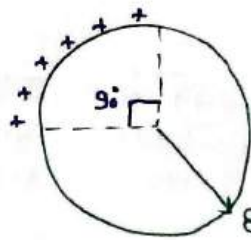
$$E = \frac{2k\lambda}{R} \sin\left(\frac{360}{2}\right)$$

$$E = \frac{2k\lambda}{R}$$



$$E_{net} = 2(E)_{half}$$

$$2 \left(\frac{2k\lambda}{R} \right)$$

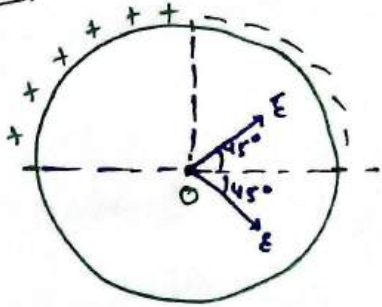


$$E = \frac{2k\lambda}{2} \sin\left(\frac{90^\circ}{2}\right)$$

$$E = \frac{2k\lambda}{2} \sin 45^\circ$$

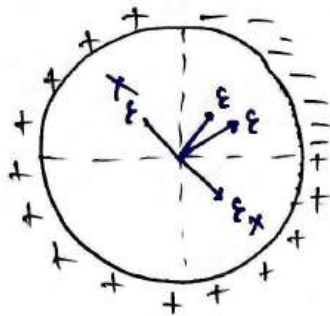
$$E = \frac{\sqrt{2}k\lambda}{R}$$

Ques 11T Maso



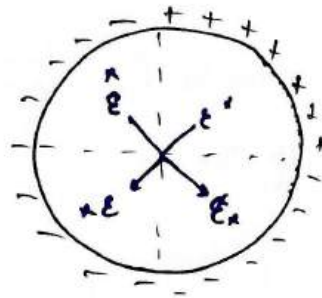
dirsn of electric field along

- (a) +y axis (b) +x axis (c) -y axis (d) y-x plane



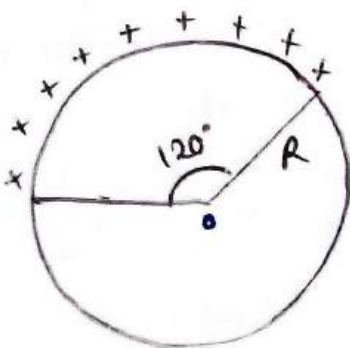
$$E_0 = 2(E)_{one fourth ring}$$

$$2 \left(\frac{\sqrt{2}k\lambda}{R} \right)$$



$$E_{net} = 0$$

Ques

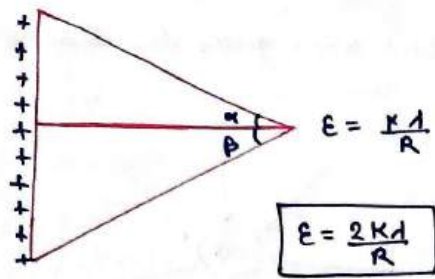


$$E_0 = \frac{2k\lambda}{R} \sin\left(\frac{\theta}{2}\right)$$

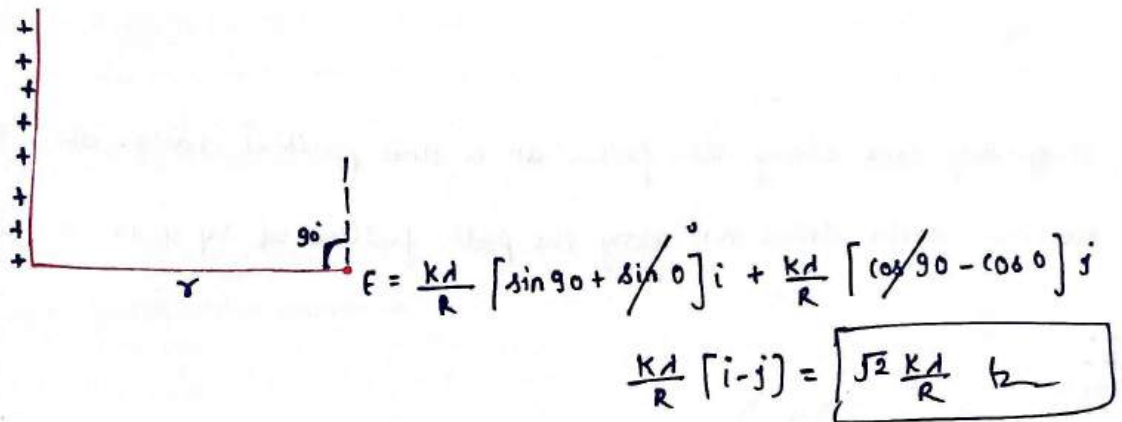
$$\frac{2k\lambda}{R} \sin\left(\frac{120^\circ}{2}\right) = \frac{2k\lambda}{2} \times \frac{1}{2}$$

$$\frac{\sqrt{3}k\lambda}{R}$$

Electric field due to finite line charge of linear density λ .



Semi-infinite line charge



Ques

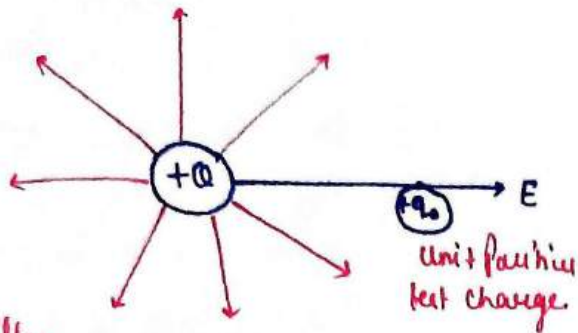
- ① $\frac{2\lambda}{\epsilon_0 a}$
- ② $\frac{\lambda\pi}{\epsilon_0 a}$
- ③ $\frac{\lambda}{2\pi\epsilon_0 a}$
- ④ $\frac{\lambda}{\pi\epsilon_0 a}$

Electric field lines

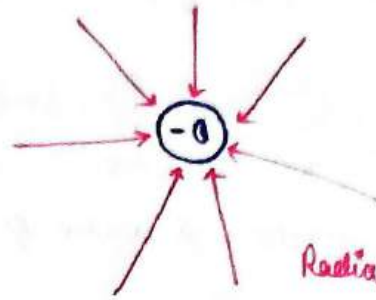


Electric field lines are the imaginary lines, tangent to which gives the direction of electric field.

- and no. of field lines passing through per unit area gives the strength of field.



Radially Outward.



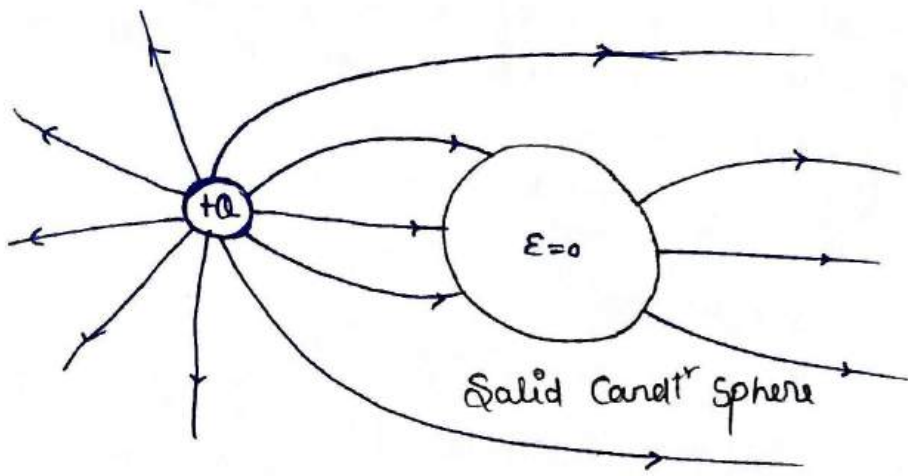
Radially Inward.

1. Imaginary line along the force on a unit positive charge also called
2. electric field lines not along the path followed by unit +ve charge.

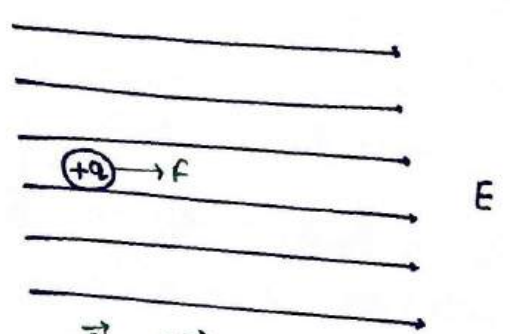


3. Start from +ve charge, end at -ve charge
4. The tangent at any point on the electric field lines gives the direction of field
5. Radially outward from positive charge and radially inward negative charge
6. Do not intersect two lines
7. Magnitude of charge \propto no. of field lines starting from that charge
8. Magnitude of electric field is directly proportional to field line density
9. always perpendicular to the surface of conductor
10. Inside isolated conductor electric field line is zero
11. Sharp turn is not possible, always continuous at all point
12. Never forms close loop.
13. It is conservative field





Motion of charge particle in Uniform electric field



Uniform acceleration (const)

$$\vec{F} = q\vec{E}$$

$$m\vec{a} = q\vec{E}$$

$$\vec{a} = \frac{q\vec{E}}{m}$$

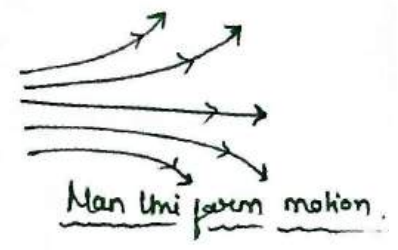
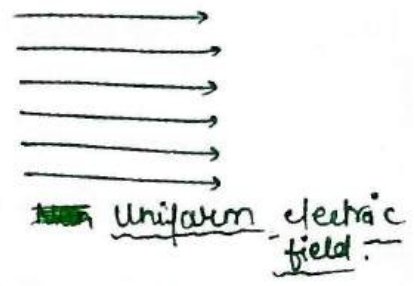
$$a = \frac{qE}{m}$$

Motion with const accelⁿ

$$a = \frac{qE}{m}$$

$$v = u + at$$

$$v = \frac{qEt}{m}$$



$$p = mu = m \frac{qEt}{m}$$

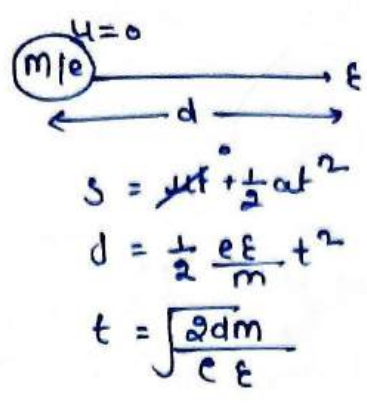
$$p = qEt$$

Ques The magnitude of force exerted by a uniform electric field on an electron having mass m_e and proton of mass m_p are represented as f_e and f_p respectively are related as.

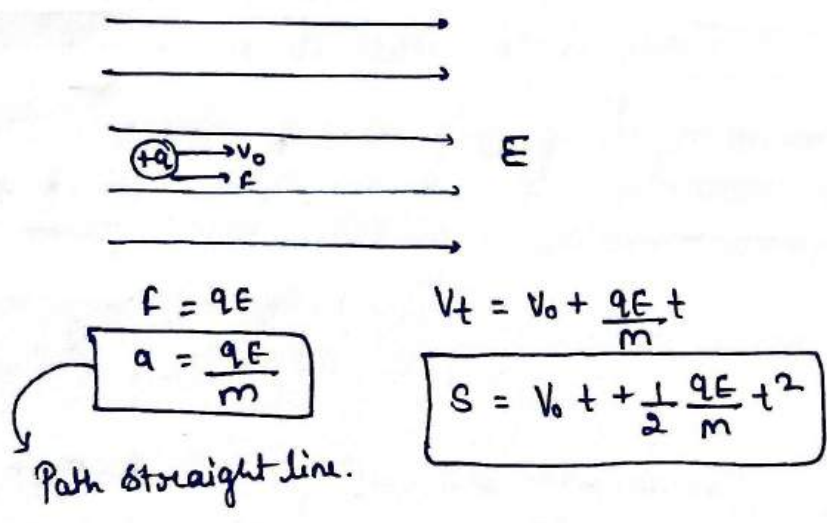
① $f_p = f_e$ \equiv

Ques A proton of mass m charge ' e ' is released from rest in a uniform electric field of strength ' E '. The time taken by it to travel a distance ' d ' in the field is

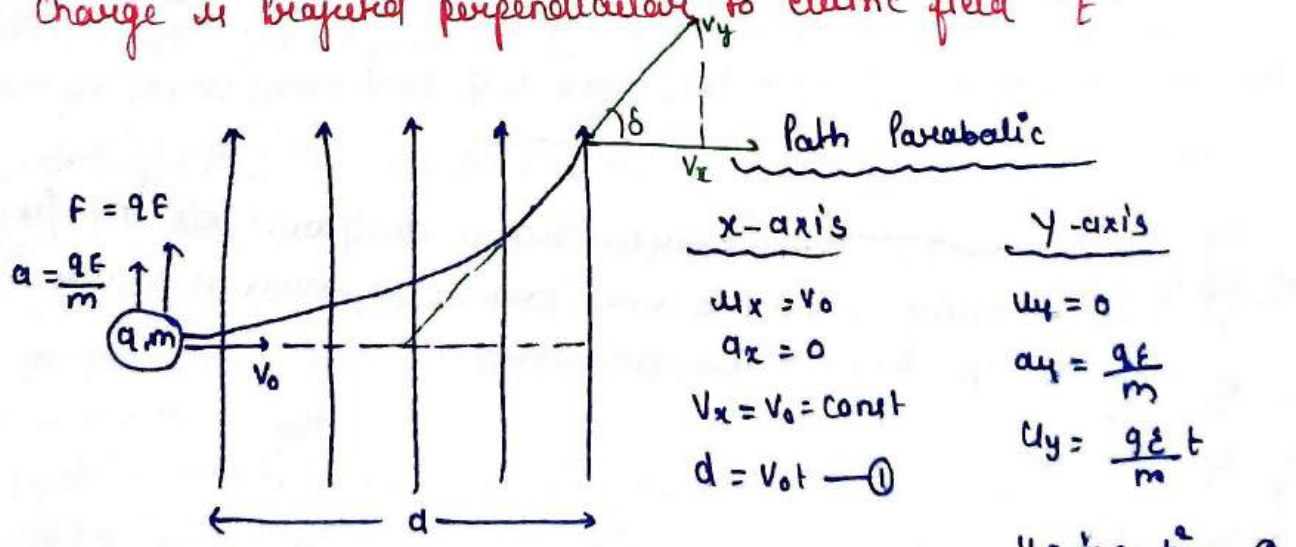
- ① $\sqrt{\frac{2de}{mE}}$
- ② $\sqrt{\frac{2dE}{me}}$
- ③ $\sqrt{\frac{2dm}{eE}}$
- ④ $\sqrt{\frac{2Ee}{m}}$



Case-2 Charge is projected parallel to electric field ' E '.



Case-3 Charge is projected perpendicular to electric field ' E '.

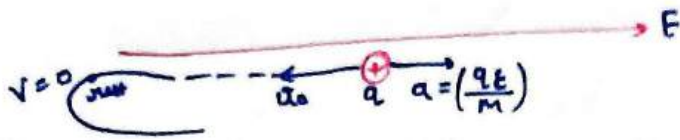


$\tan \delta = \frac{v_y}{v_x} = \frac{qEt}{mv_0}$
 $\tan \delta = \frac{qEt}{mv_0}$

$\tan \delta = \frac{qEd}{mv_0^2}$
 $\delta = \tan^{-1} \left(\frac{qEd}{mv_0^2} \right)$

3. Charge particle placed in uniform electric field at rest

charge is projected opposite to electric field find stopping distance



Path is straight line

$$v_p^2 - u_0^2 = 2Sa$$

$$-u_0^2 = 2\left(\frac{qE}{m}\right)S$$

$$S = \frac{-u_0^2}{2\left(\frac{qE}{m}\right)}$$

Ques A mass m carrying a charge q is suspended from a string and placed in a uniform horizontal electric field of intensity E . The angle made by the string with the vertical in the equilibrium position is.

① $\theta = \tan^{-1} \frac{mg}{Eq}$

② $\theta = \tan^{-1} \frac{m}{Eq}$

③ $\theta = \tan^{-1} \frac{Eq}{m}$

④ $\theta = \tan^{-1} \frac{Eq}{mg}$ ✓

$$\tan \theta = \frac{qE}{mg}$$

$$\theta = \tan^{-1} \frac{qE}{mg} \quad \underline{\underline{\text{Ans}}}$$

Ques In a uniform electric field if a charge is fired in a direction different from the line of electric field then the trajectory of the charge will be a.

① Straight line

② Circle

③ Parabola ✓

④ Ellipse

Ques A positively charged pendulum is oscillating in a uniform electric field pointing upwards. its time period as compared to that when it oscillate without electric field.

- ① is less
- ② is more ✓
- ③ Remains unchanged
- ④ Starts fluctuating

Ques Two equal positive charges Q are fixed at points $(a, 0)$ and $(-a, 0)$ on the x -axis. An opposite charge $-q$ at rest is released from point $(0, a)$ on the y -axis. The charge $-q$ will

- ① move to infinity
- ② move to origin and rest there
- ③ Undergo SHM about the origin
- ④ Execute oscillatory periodic motion but not SHM ✓

Ques A particle of mass m and charge q is placed at rest in a uniform electric field E and then released. the kinetic energy attained by the particle moving a distance y is.

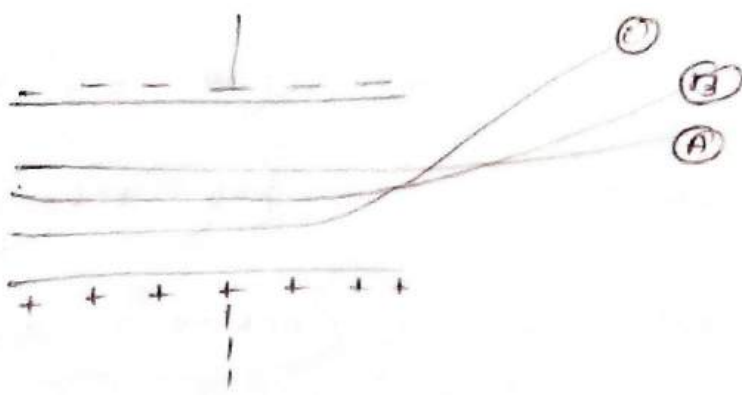
- ① qEy ✓
 - ② qE^2y
 - ③ qEy^2
 - ④ q^2Ey
- $K \cdot E = W = F \times d$
 $= qEy$

Ques A proton and an α particle having equal kinetic energy are projected in a uniform transverse electric field as shown in figure

- ① proton trajectory is more curved
- ② α -particle trajectory is more curved ✓
- ③ Both trajectories are equally curved but in opposite direction
- ④ Both trajectories are equally curved and in same direction

Ques Three particles are projected in a uniform electric field with same velocity perpendicular to the field as shown which particle has highest charge to mass ratio?

- ① A
- ② B
- ③ C
- ④ all have charge to mass ratio



Ques A particle of mass m and charge q is thrown at a speed u against a uniform electric field E . How much distance will it travel before coming to rest?

- ① $mu^2 / 2qE$ ✓
- ② $2mu^2 / qE$
- ③ $mqE / 2u^2$
- ④ mu / qE

$$s = \frac{u^2}{2 \left(\frac{qE}{m} \right)}$$

Ques If electron and proton released in electric field find ratio of momentum after time 't'.

- (a) $m_p : m_e$
- (b) $m_e : m_p$
- (c) $\sqrt{m_e} : \sqrt{m_p}$
- (d) $1 : 1$ ✓

Ques Proton, deuteron and α -particle projected in electric field, perpendicular to it then find ratio of deviation if

- ① Velocity of projection is same
- ② K.E of projection same
- ③ Projected with same momentum.

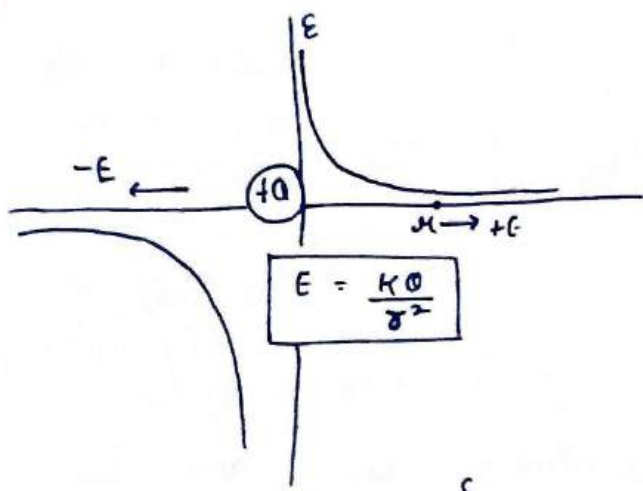
② $\tan \delta = \frac{qEd}{mV_0^2}$
 $\tan \delta = q$
 $\delta_p : \delta_D : \delta_\alpha = e : e : 2e$
 $1 : 1 : 2$

① $\delta_p : \delta_D : \delta_\alpha = \frac{p}{m} : \frac{p}{2m} : \frac{p}{4m}$
 $= 2 : 1 : 1$

③ $\tan \delta = \frac{qEd}{(mV_0^2)}$
 $\frac{maEd}{p^2}$
 $\tan \delta \propto mq$

$\tan \delta = \frac{qEd}{mV_0^2} \propto \frac{q}{m}$

$\delta_p : \delta_D : \delta_\alpha = e : 2e : 8e$
 $= 1 : 2 : 8$ ✓



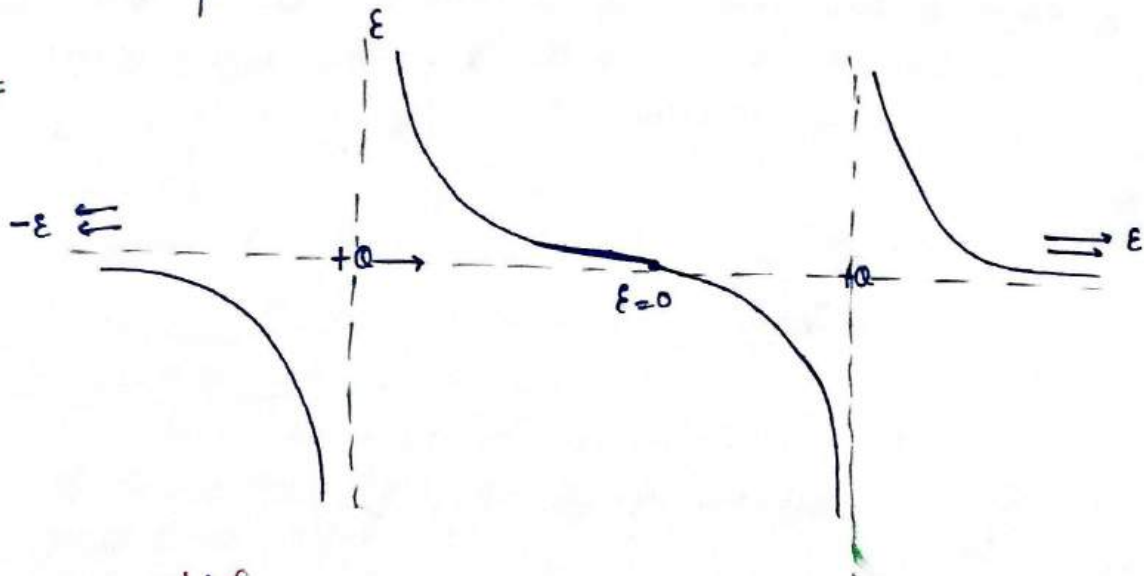
IF

$+Q \quad E=0 \quad +Q$

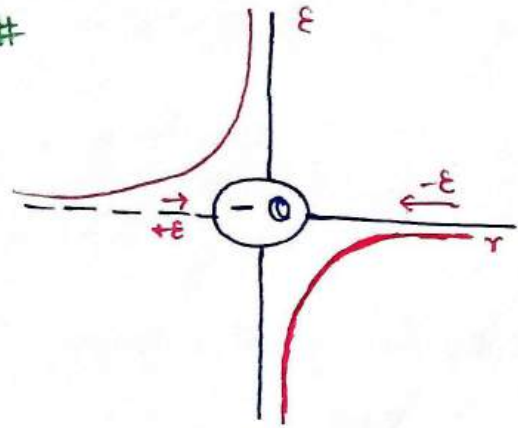
$+Q \quad E=0 \rightarrow +\frac{Q}{8}$

$E=0 \quad +Q \quad -8Q$

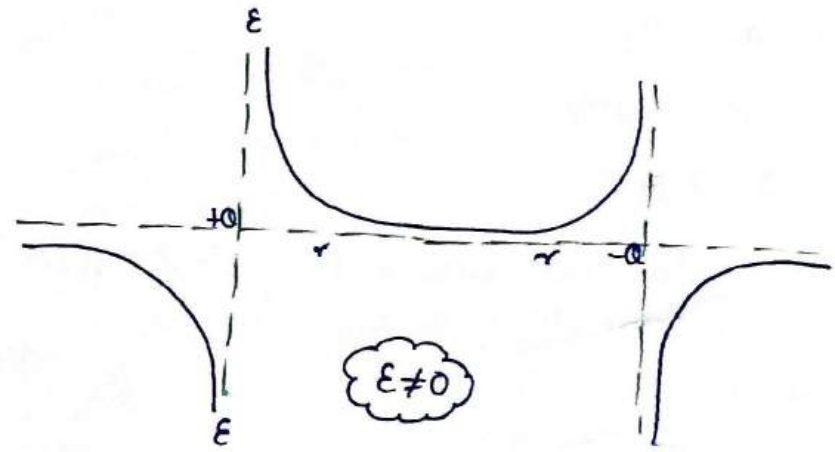
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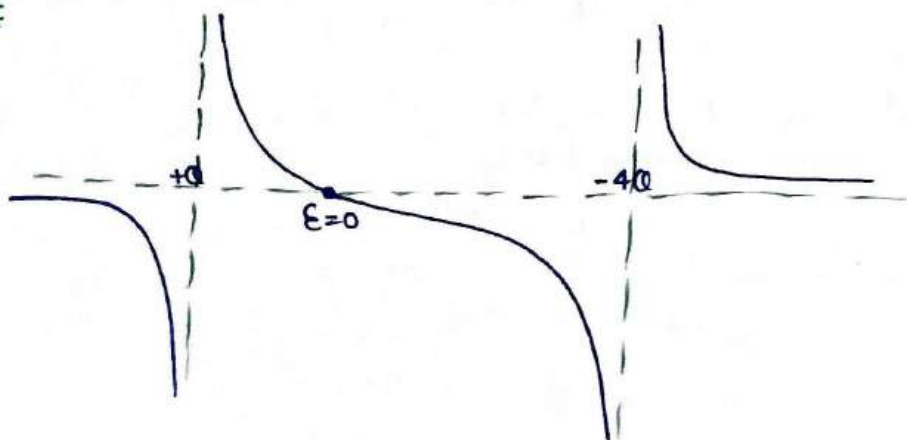
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#



#



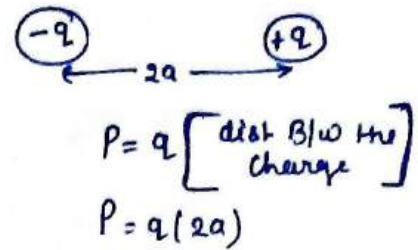
#

$+Q \quad -Q$

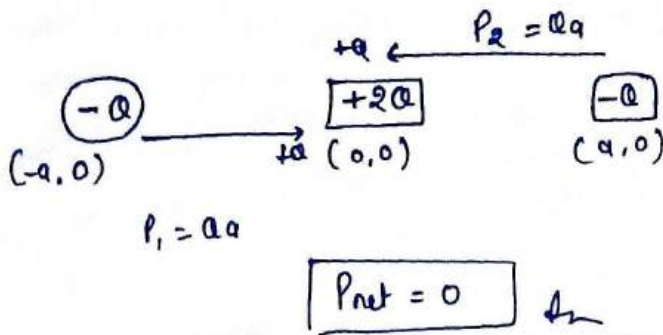
dipole - Combination of two equal & opposite charge placed at same dist

Electric dipole

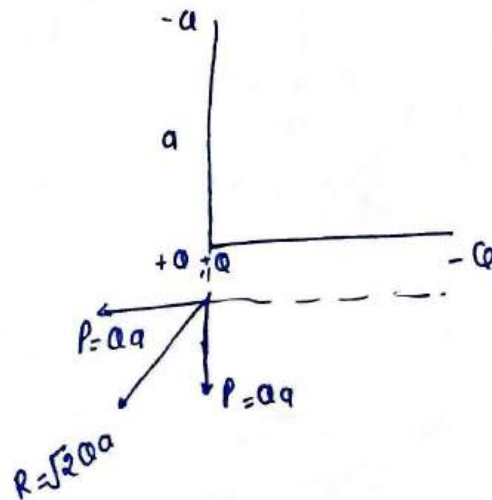
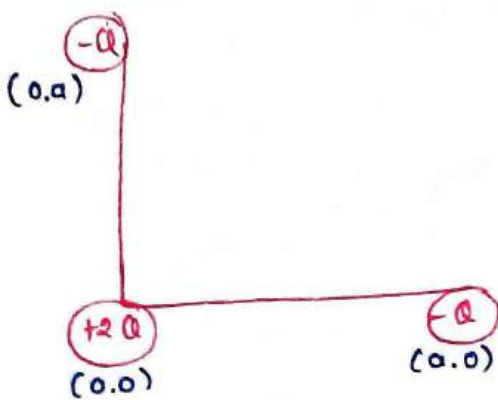
Pair of equal and opposite charge q and $-q$ separated by a small distance ' r ' then electric dipole moment is defined along $-q$ to $+q$.



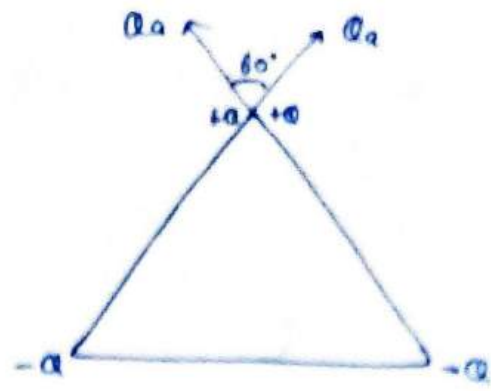
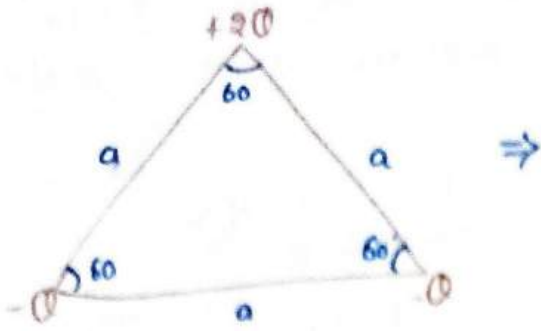
- = Vector
- = direction from $-q$ to $+q$ charge
- = Coulomb-meter (cm)
- = $[A^1 T^2 L^1]$



Net electric dipole moment

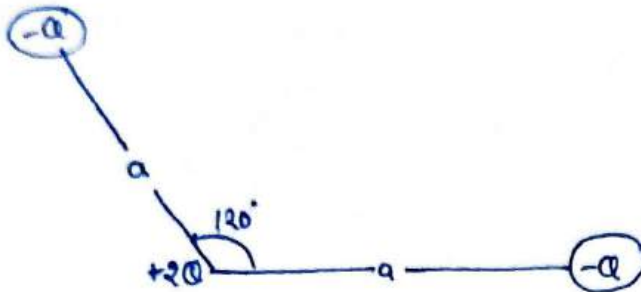


Q Find net electric dipole moment ?



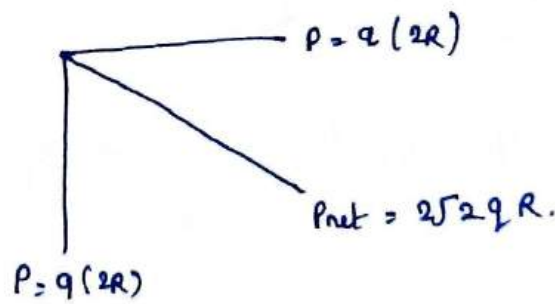
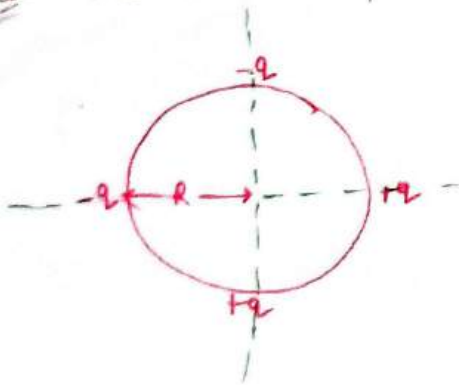
$P_{net} = \sqrt{3} Q a$ Ans

Q Find net electric dipole moment ?

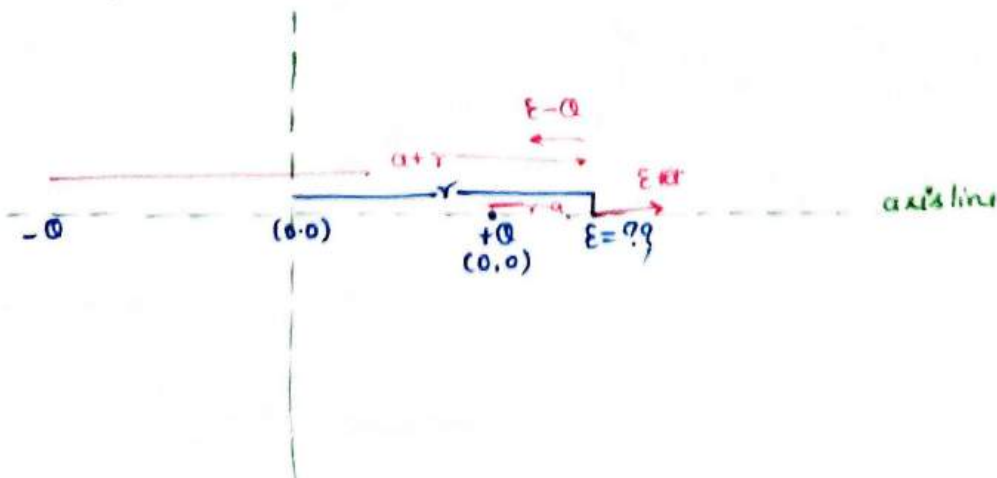


$P_{net} = Q a$

Q Net electric dipole moment ?



Electric field due to dipole



$$\begin{aligned} \vec{E}_{net} &= \vec{E}_{+a} - \vec{E}_{-a} \\ &= \frac{kQ}{(r-a)^2} - \frac{kQ}{(r+a)^2} \\ &= kQ \left[\frac{(r+a)^2 - (r-a)^2}{(r^2-a^2)^2} \right] \\ &= kQ \left[\frac{r^2+a^2+2ra - r^2+a^2-2ra}{(r^2-a^2)^2} \right] \\ F &= \frac{4kQra}{(r^2-a^2)^2} \end{aligned}$$

$$E_{axial} = \frac{4kQar}{(a^2-r^2)^2}$$

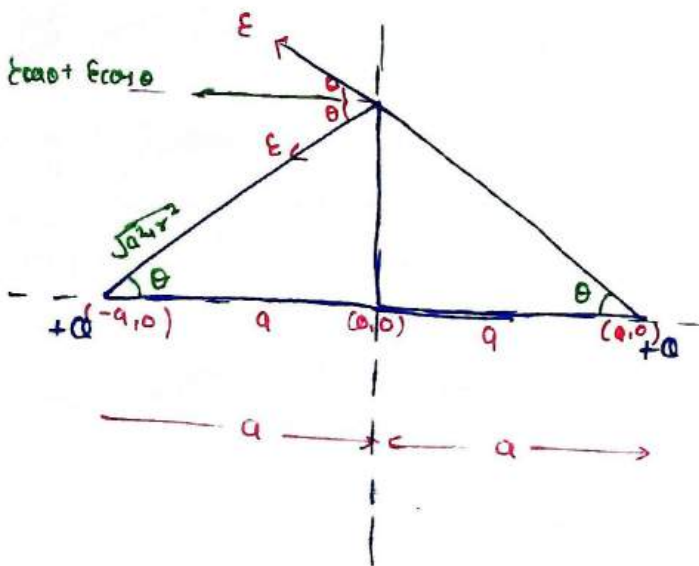
$$\vec{E}_{axis} = \frac{2kPr}{(r^2-a^2)^2}$$

dipole is small ($a \ll r$)

$$\vec{E}_{axis} = \frac{2kP}{r^3}$$

~~small dipole ($a \ll r$)~~

Electric field due to dipole =



$$\begin{aligned} E_{net} &= 2E \cos \theta \\ &= 2 \frac{kQ}{(a^2+r^2)} \times \frac{a}{(a^2+r^2)^{1/2}} \end{aligned}$$

$$\vec{E}_{net} = \frac{2kQa}{(a^2+r^2)^{3/2}}$$

$$E = \frac{kP}{(a^2+r^2)^{3/2}}$$

Small dist ($a \ll r$)

$$\vec{E} = \frac{-kP}{r^3}$$

equator

$$\vec{E} = \frac{-K\vec{p}}{r^3} = \frac{2KQa}{(r^2+a^2)^{3/2}}$$

$$\vec{E}_{\text{axis}} = \frac{2Kp}{r^3} = \frac{4KQa\gamma}{(r^2-a^2)^2}$$

$$\frac{\vec{E}_{\text{axial}}}{\vec{E}_{\text{equat}}} = \frac{\frac{2Kp}{r^3} \times \frac{1}{\sqrt{3}}}{\frac{-1Q}{r^3}} = \frac{2}{-1}$$

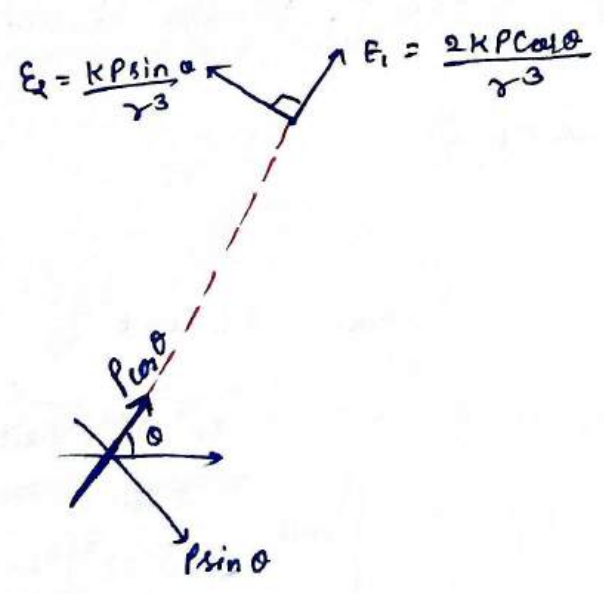
$p = Q \cdot 2a$

$$\vec{E} = \frac{-2KQa}{(r^2+a^2)^{3/2}} = \frac{-Kp}{r^3}$$

$$\vec{E} = \frac{4KQa\gamma}{(r^2-a^2)^2} = \frac{2Kpr}{(r^2-a^2)^2}$$

$$= \frac{2Kp\gamma}{r^3} = \left(\frac{2Kp}{r^3}\right)_B$$

Electric field due to dipole at general point \Rightarrow



Ques A electric field always along dipole moment on the axial line
B electric field always anti parallel to the dipole moment on equi axial line

1. Both true
2. Both false
3. A (true) B (false)
4. A (false) B (true) ✓✓

Ques Two charges of $+25 \times 10^{-9}$ Coulomb and -25×10^{-9} Coulomb are placed 6 m apart. find the electric field intensity ratio at points 4 m from the centre of the electric dipole (i) as

① $\frac{1000}{49}$ ✓

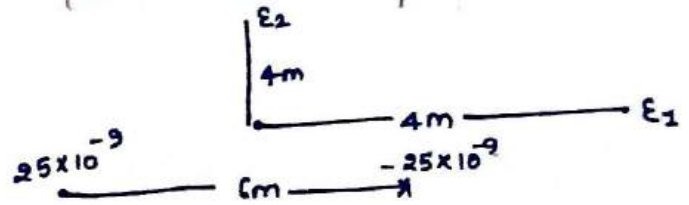
② $\frac{49}{1000}$

③ $\frac{500}{49}$

④ $\frac{49}{500}$

$$E_1 = \frac{4kQq}{(a^2 - r^2)^2}$$

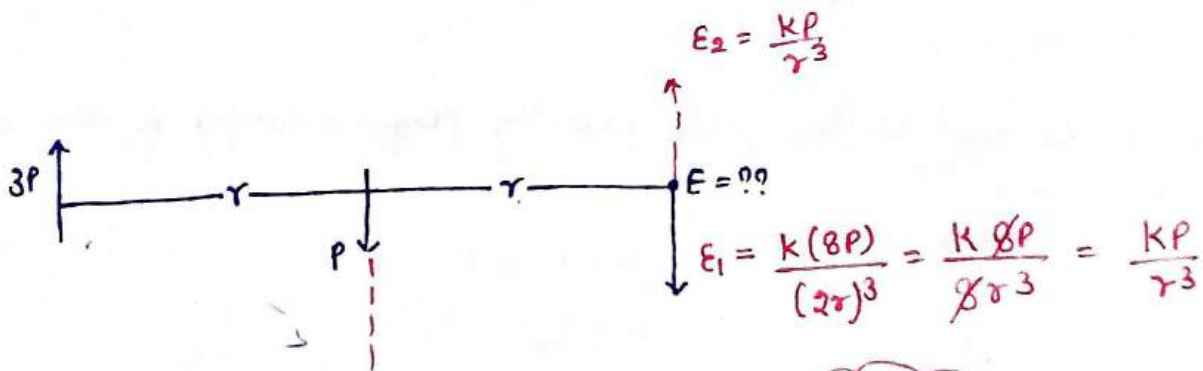
$$E_1 = \frac{4kQq}{(3^2 - 4^2)^2}$$



$$E_2 = \frac{2kQq}{(a^2 + r^2)^{3/2}} = \frac{2kQq}{(3^2 + 4^2)^{3/2}}$$

$$\frac{E_1}{E_2} = \frac{2 \times 4 \times (25)^{3/2}}{49} = \frac{4 \times 2 \times 125}{49} = \frac{1000}{49}$$

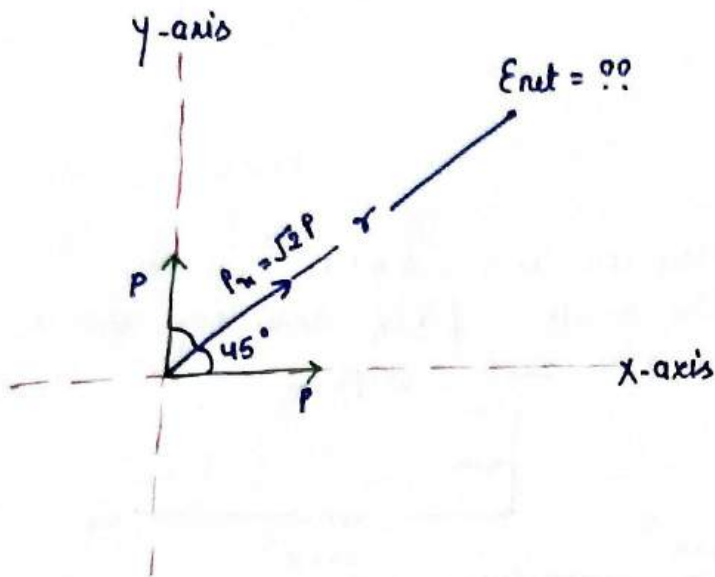
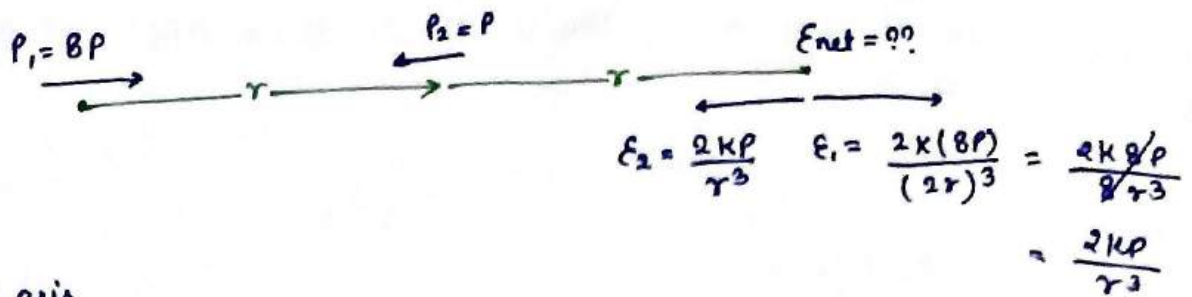
Small dipole = Ideal dipole



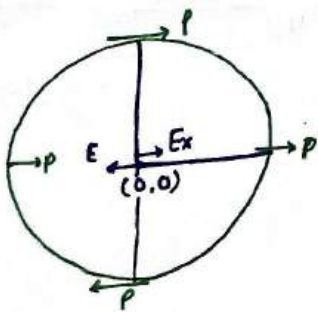
$$E_2 = \frac{kP}{r^3}$$

$$E_1 = \frac{k(8P)}{(2r)^3} = \frac{k8P}{8r^3} = \frac{kP}{r^3}$$

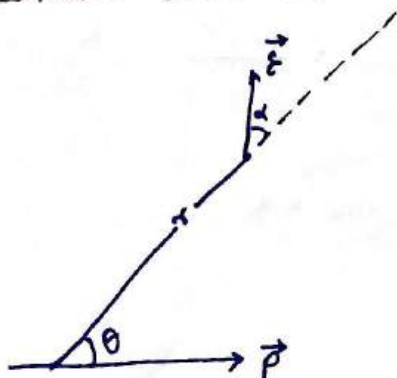
$E_{net} = 0$



Net electric field at origin ??



Ans Find ' θ ' so that electric field exactly perpendicular to the dipole moment vector ??



$$\alpha + \theta = 90^\circ$$

$$\alpha = (90 - \theta)$$

taking tan both side

$$\tan \alpha = \tan (90 - \theta)$$

$$\frac{\tan \theta}{2} = \cot \theta = \frac{1}{\tan \theta}$$

$$\tan^2 \theta = 2$$

$$\tan \theta = \sqrt{2}$$

$$\theta = \tan^{-1} \sqrt{2}$$

Ans

Ques electric force b/w dipole & charge is F , new distⁿ b/w them becomes double the force will become.

- (a) same
 (b) one fourth
 (c) 4 - times
 (d) $\frac{1}{8}$ times



$$F = qE_{dipole}$$

$$E = \frac{q_2 k p}{r^3}$$

$$E \propto \frac{1}{r^3}$$

force b/w two point charge
 $F \propto \frac{1}{r^2}$

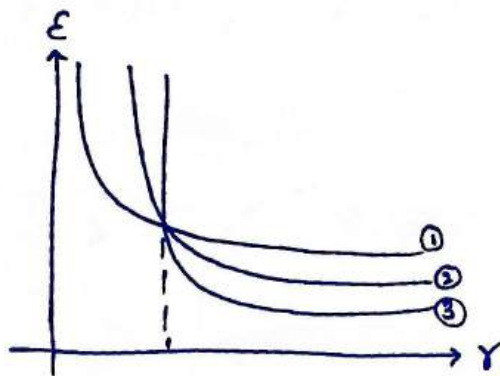
force b/w dipole & point charge
 $F \propto \frac{1}{r^3}$

force b/w two dipole
 $F \propto \frac{1}{r^4}$

Electric force b/w two dipole is F , new distⁿ b/w them becomes double the force will become.

- ① Same
 ② one fourth
 ③ $\frac{1}{16}$ time
 ④ $\frac{1}{8}$ time

$$F \propto \frac{1}{r^4} \quad F' \propto \frac{1}{(2r)^4} = \frac{F}{16r^2}$$



$$E_{point} \propto \frac{1}{r^2}$$

$$E_{line} \propto \frac{1}{r}$$

$$E_{dipole} \propto \frac{1}{r^3}$$

Graph	field
(P)	dipole electric field
(Q)	Electric field due to Point charge
(R)	electric field of Line charge

Electric Flux \Rightarrow

- It gives the idea of electrostatic energy passing through given area
- Counting of electric field lines passing through given cross section area
- \rightarrow Scalar Unit - Nm^2/C

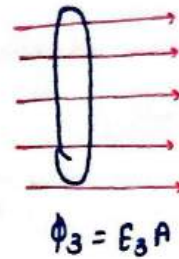
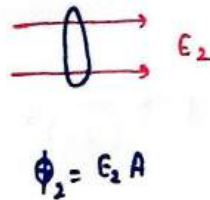
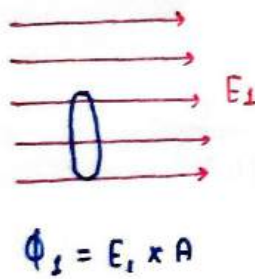
$E = \text{Uniform}$ $\phi = \vec{E} \cdot \vec{A}$ Nm^2/C

$$\phi = EA \cos \theta$$

Electric field $\vec{E} = 2\hat{i} + 3\hat{j} + 4\hat{k}$ then find flux through an rod of length 5 m placed along 'y' axis.

- (a) 10 (67%)
- (b) 15 (50%)
- (c) 40 (67%)
- (d) Not possible

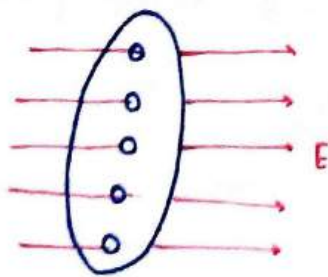
$$\phi = \vec{E} \cdot \vec{A}$$



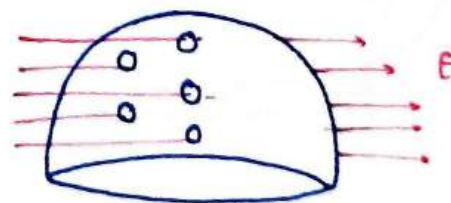
$$\phi_3 > \phi_1 > \phi_2$$

$$\phi_1 > \phi_2$$

Electric Flux



Disc / Ring / Square

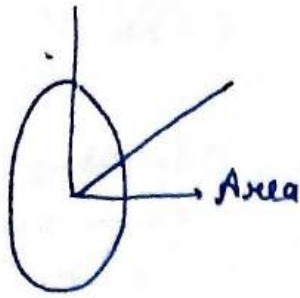


Hemisphere

$$\phi \text{ Passing through} = \vec{E} \cdot \vec{A}$$

Ques

Electric field $E = 50 \text{ N/C}$ & Area is 20 m^2 & Angle b/w electric field & surface is 30° then find flux?



$$\begin{aligned} \phi &= EA \cos \theta \\ &= 50 \times 20 \times \cos 60^\circ \\ &= 50 \times \frac{20}{2} \times \frac{1}{2} \\ &= \boxed{500 \text{ } \cancel{\text{N}} \cdot \text{m}^2/\text{C}} \end{aligned}$$

Non-Uniform field

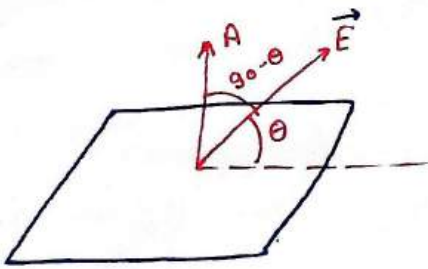
$$\begin{aligned} \int d\phi &= \int E \cdot dA \\ \phi &= \int E \cdot dA \end{aligned}$$

$$\begin{aligned} \phi &= (E_x \hat{i} + E_y \hat{j} + E_z \hat{k}) \cdot (A_x \hat{i} + A_y \hat{j} + A_z \hat{k}) \\ &= E_x A_x + E_y A_y + E_z A_z \end{aligned}$$

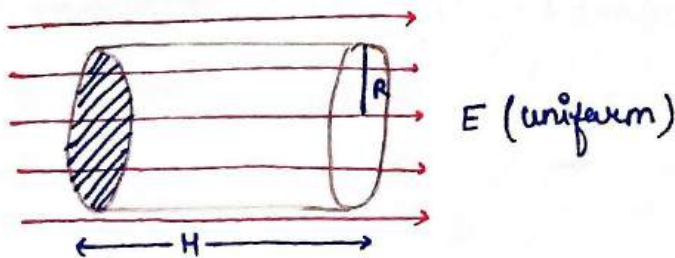
Angle b/w surface & electric field is θ

$$\phi = EA \cos (90 - \theta)$$

* Angle b/w Area & surface is always 90°



Ques Find incoming and outgoing flux through cylinder.



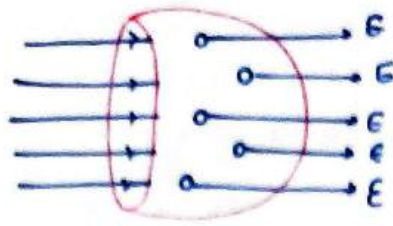
$$\begin{aligned} \phi_{in} &= E \pi R^2 \cos 180^\circ \\ &= -E \pi R^2 \end{aligned}$$

$$\phi_{total} = \phi_{in} + \phi_{out} = 0$$

$$\begin{aligned} \phi_{out} &= E \pi R^2 \cos 0^\circ \\ &= E \pi R^2 \end{aligned}$$

Ques The flux through the hemispherical surface in the figure shown below is

- ① $\pi R^2 E$ ✓
- ② $2\pi R^2 E$
- ③ $\pi R E$
- ④ zero



$$\phi = E \times \pi R^2 \times X$$

$$\# \phi_{\text{total}} = \phi_{\text{in}} + \phi_{\text{out}} = 0$$

$$-\pi R^2 E + \phi_{\text{out}} = 0$$

$$\boxed{\phi = \pi R^2 E} \quad R$$

$$\text{Area} = \frac{4\pi R^2}{2} = 2\pi R^2.$$

Ques A cylinder of radius R and length l is placed in a uniform electric field E parallel to

Ques A rectangular surface of sides

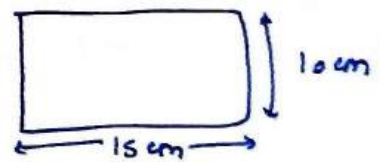
1. $0.1675 \text{ N/m}^2 \text{ C}$
2. $0.1875 \text{ N/m}^2 \text{ C}$
3. zero
4. 0.107

$$\phi = EA \cos \theta$$

$$25 \times 10 \times 15 \times 10^{-4} \times \cos 15$$

$$25 \times 10^5 \times 15 \times 10^{-4} \times \frac{1}{2}$$

$$125 \times 15 \times 10^{-4}$$



Ques If an electric field is given by $10\hat{i} + 3\hat{j} + 4\hat{k}$

- ① 100 unit
- ② 10 unit
- ③ 30 unit
- ④ 40 unit

Ques

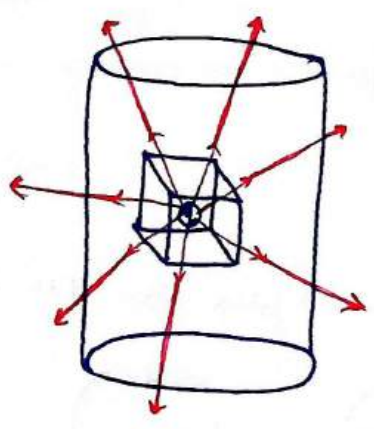
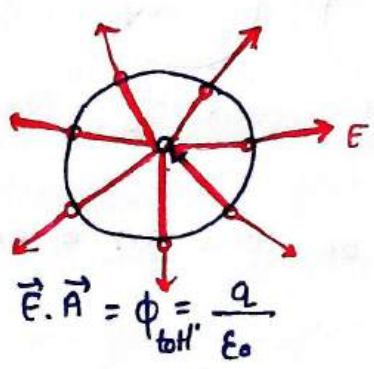
There is uniform electric field of 8×10^3

Gauss Law →

The total flux passing through any close surface is equal to $\frac{q}{\epsilon_0}$ where q is total enclosed charge.

Disc.
Ring
Surface from
(Not valid)

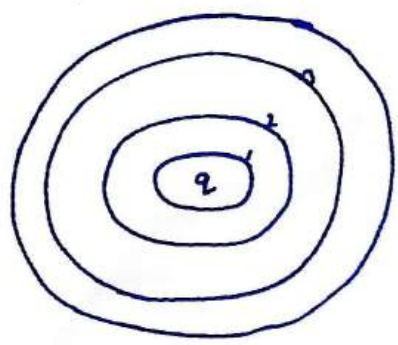
Ex! Close surface
Sphere, Cylinder, Cube



$\phi_{\text{sphere}} = \phi_{\text{cube}} = \phi_{\text{cylinder}}$

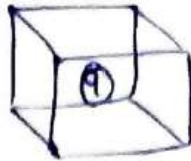
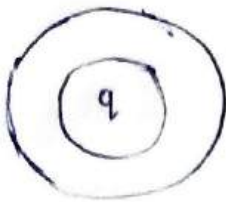
The electric flux passing through a closed surface 's' is equal to $\frac{q}{\epsilon_0}$ where q is total charge enclosed by surface

$\phi_1 = \phi_2 = \phi_3 = \phi_4$

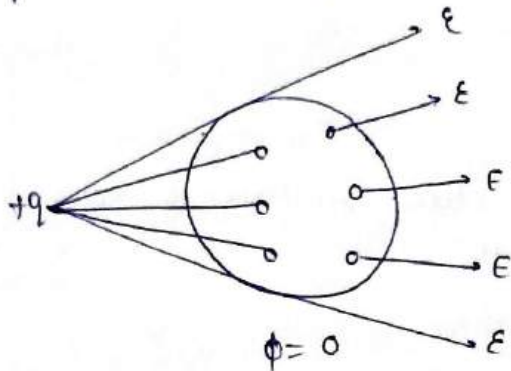


Important Points

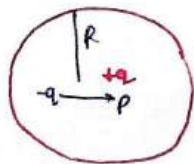
1. Gauss law is true for any closed surface, no matter what its shape or size only depend on charge enclosed.



2. If no charge is enclosed then total flux must be zero, it does not depend on charge present outside the surface.

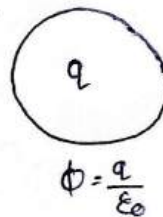


Ques

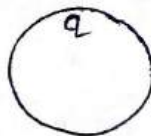
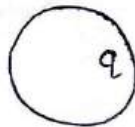


$$\phi_{\text{sphere}} = 0$$

Ex:



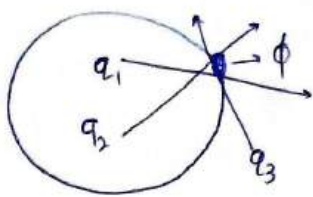
3. Flux through closed surface does not depend on location of enclosed charge.



4. Gauss law is always valid, but it may not be useful to calculate electric field for closed surface.

$$\phi = \frac{q_{\text{in}}}{\epsilon_0} = \oint \vec{E} \cdot d\vec{A}$$

Gauss is always valid and always useful to calculate flux, but not always useful to calculate electric field.



$$\Phi_{\text{total}}^{\text{Gauss}} = \left(\frac{q_1 + q_2}{\epsilon_0} \right) = \oint \vec{E} \cdot d\vec{A}$$

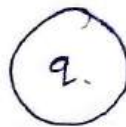
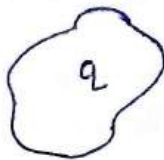
due to all the charge q_1, q_2, q_3 whether inside or outside

$$\phi = \frac{q_{\text{in}}}{\epsilon_0} = \int \vec{E} \cdot d\vec{A}$$

q_{in} - enclosed charge
 \vec{E} = due to all charge

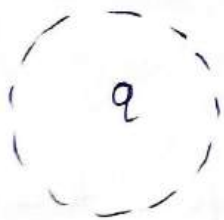
In Gauss law is valid for both Gaussian surface?

- ① Yes ✓
- ② No
- ③ Can't say



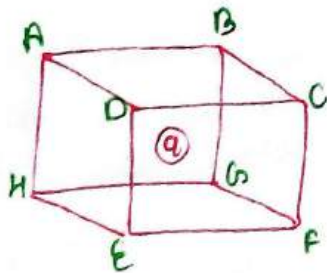
5. Gaussian Surface

Gauss law useful and easy to calculate electric field when system have some symmetry. This is achieved by choice of a suitable Gaussian surface



Gaussian surface - Imaginary, symmetric open surface

Ques Find flux through cube in given situation

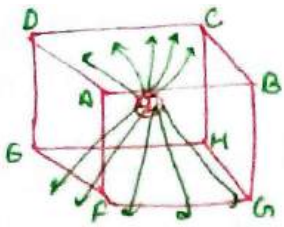


$$(\Phi_{\text{net}})_{\text{surface}} = \frac{q}{\epsilon_0}$$

Ans

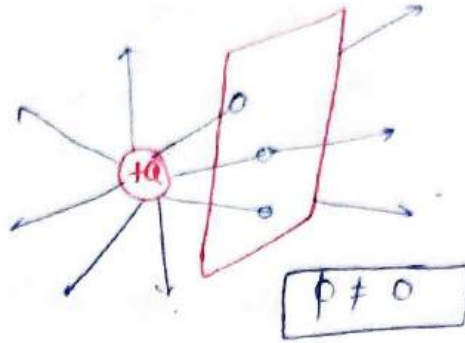
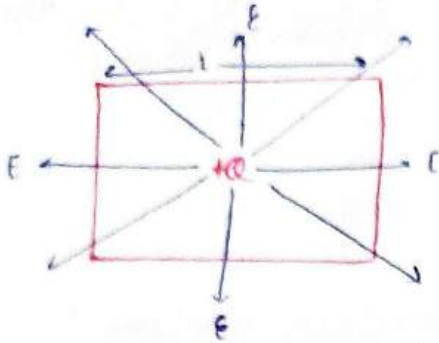
$$\phi_{\text{cube}} = \frac{q_{\text{enclosed}}}{\epsilon_0} = \frac{q}{\epsilon_0} = 6 \phi_{\text{one flux}}$$

Ques



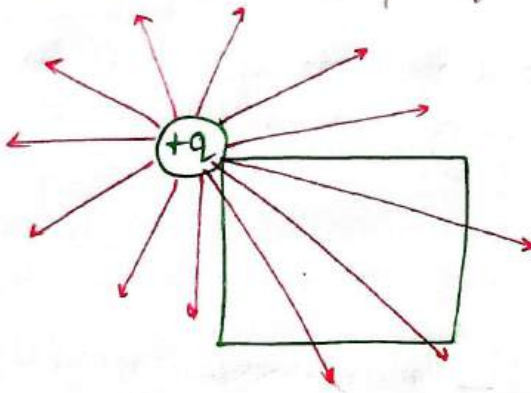
$$\phi_{\text{ABCD}} > \frac{q}{6\epsilon_0}$$

Ans



Charge +q is placed at
Centre of square plate
 $\phi = 0$

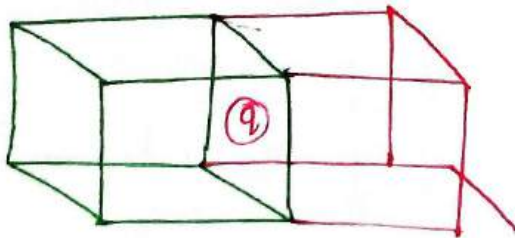
Ques Charge is at corner of square plate



$$\phi_{\text{square plate}} = 0$$

Ques

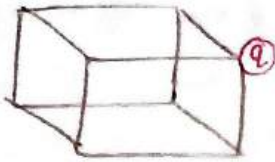
Charge is placed at centre of one face then flux through cube ?



$$\phi_{\text{cube}} = \frac{q}{\epsilon_0}$$

$$\phi_{\text{cube}} = \frac{q}{2\epsilon_0}$$

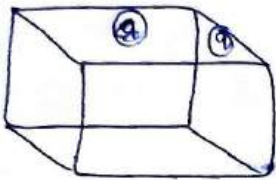
Ques Charge is at corner of cube?



$$8 \phi_{\text{cube}} = \frac{q}{\epsilon_0}$$

$$\phi_{\text{cube}} = \frac{q}{8\epsilon_0}$$

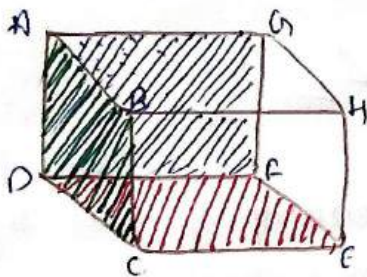
Ques Charge is at mid of side



$$4 \phi_{\text{cube}} = \frac{q}{\epsilon_0}$$

$$\phi_{\text{cube}} = \frac{q}{4\epsilon_0}$$

Ques Find flux passing through face ABCD of this cube??



$$\phi_{\text{cube}} = \frac{q}{8\epsilon_0}$$

$$\phi_{\text{cube}} = \frac{q}{8\epsilon_0} = 3(\phi_{\text{ABCD}})$$

$$\phi_{\text{ABCD}} = \frac{q}{24\epsilon_0}$$

$$\phi_{\text{HBAG}} = \phi_{\text{EFGH}} = \phi_{\text{HBCF}} = 0$$

Ques A hollow cylinder has a charge q Coulombs within it. If ϕ is the electric flux in units of Voltmetre associated with the curved surface B , the flux linked with the plane surface A in unit of Voltmetre will be (charge is symmetrically placed within it)

① $\left(\frac{q}{\epsilon_0} - \phi\right)$

② $\frac{1}{2} \left(\frac{q}{\epsilon_0} - \phi\right)$

③ $\frac{q}{2\epsilon_0}$

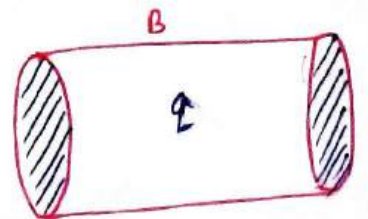
④ $\phi/2$

$$\phi_{\text{cylinder}} = \frac{q}{\epsilon_0}$$

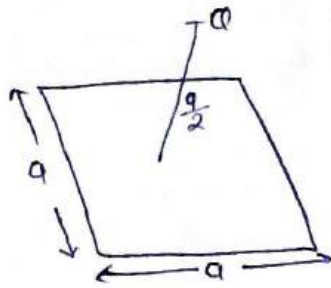
$$\phi_{\text{curved}} + 2\phi_{\text{flat}} = \frac{q}{\epsilon_0}$$

$$\phi + 2\phi_{\text{flat}} = \frac{q}{\epsilon_0}$$

$$\phi_{\text{flat}} \cdot \left(\frac{q}{\epsilon_0} - \phi\right) \frac{1}{2}$$

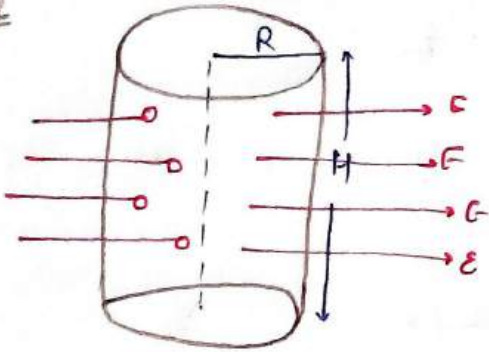


Q. A charge Q is placed at a distance $a/2$ above the centre of a horizontal square of edge 'a' as shown in figure. Find the flux of the electric field through the square surface.



$$\phi = \frac{q}{6\epsilon_0}$$

Ques



$$\phi_{\text{total}} = 0$$

ϕ Ingoing flux in cylinder from curved surface??

$$\phi = -E \cdot 2RH$$

Ques If the number of electric lines of force emerging out of a closed surface is 1000 then the charges enclosed by the surface is

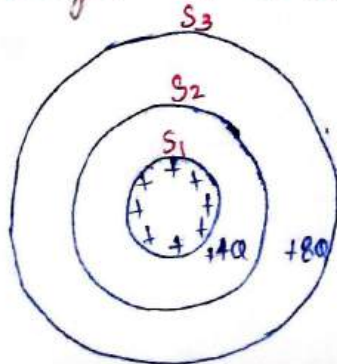
- ① $8.854 \times 10^{-9} \text{ C}$
- ② $8.854 \times 10^{-4} \text{ C}$
- ③ $8.854 \times 10^{-1} \text{ C}$
- ④ 8.854 C

$$\phi = \frac{q}{\epsilon_0} = \text{no. field line}$$

$$q = 1000 \times \epsilon_0 = 1000 \times 8.854 \times 10^{-12} = 8.854 \times 10^{-9} \text{ C}$$

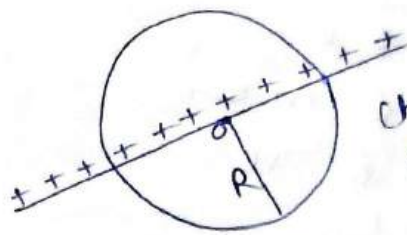
Ques S_1, S_2, S_3 are three concentric spherical shells, as shown in figure. S_1 and S_2 have charge $+Q$ and $8Q$ respectively, whereas S_3 is uncharged. Find the ratio of the flux passing through S_1 to that through S_3

- ① $1:3$
- ② $1:2$
- ③ $2:1$
- ④ $1:6$



$$\frac{\phi_{S1}}{\phi_{S2}} = \frac{4\pi Q}{\epsilon_0} \times \frac{\epsilon_0}{4\pi \cdot 8Q} = \frac{1}{8}$$

$$= \frac{1}{3}$$

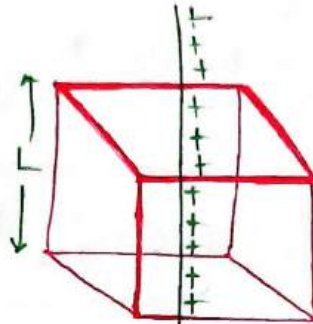


Charge on rod = λ
 $dl = \lambda dl$
 $2R = \lambda 2R$

$$\phi = \frac{q_{in}}{\epsilon_0} = \frac{\lambda 2R}{\epsilon_0}$$

Charged Rod is passing through centre of sphere having linear charge density λ . then find flux through sphere.

Q11



$$\phi_{\text{cube}} = \frac{[L\lambda]}{\epsilon_0}$$

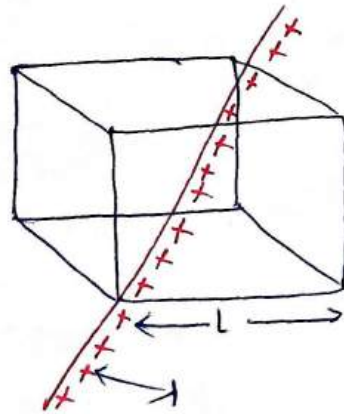
λ (charge density)

Charged Rod is placed inside cube then find maximum flux that can pass through the cube??

$$l_{\text{inside}} = \sqrt{3} L$$

$$q_{in} = \lambda \sqrt{3} L$$

$$\phi = \frac{\sqrt{3} L \lambda}{\epsilon_0}$$



Q14 Find flux through sphere

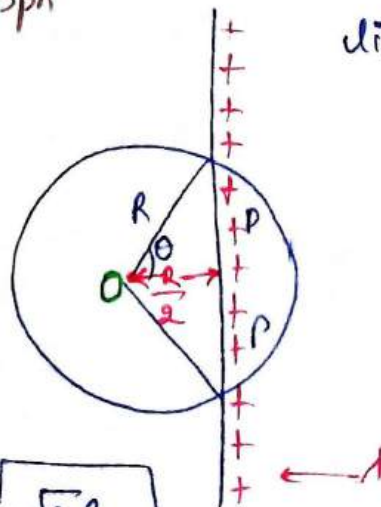
$$\sin \theta = \frac{R}{2R} = \frac{1}{2}$$

$$\theta = 30^\circ$$

$$P^2 + \frac{R^2}{4} = R^2$$

$$P^2 = R^2 - \frac{R^2}{4} = \frac{3R^2}{4} \Rightarrow$$

$$P = \frac{\sqrt{3} R}{2}$$



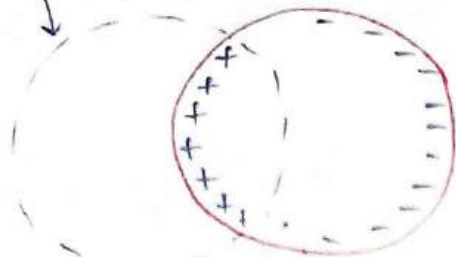
$$l_{\text{inside}} = 2P = \sqrt{3} R$$

$$P = \frac{\sqrt{3} R}{2}$$

$$P = \frac{\sqrt{3} R}{2}$$

Find flux passing through gaussian surface

Closed gaussian surface

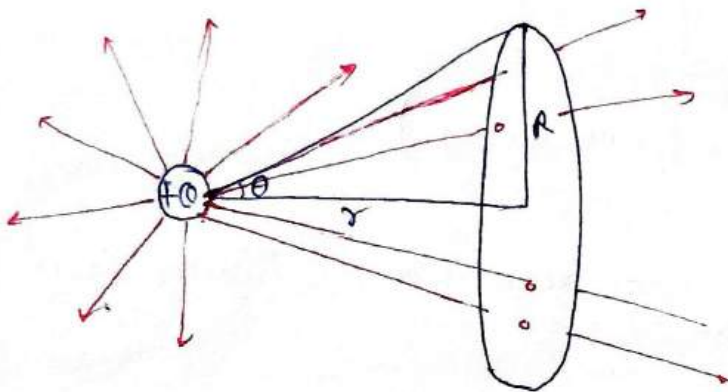


(Neutral sphere)

$$Q_{net} = 0$$

- (a) $\phi = 0$
- (b) $\phi = +ve$ ←
- (c) $\phi = -ve$
- (d) None

Find flux passing through disc of radius R.



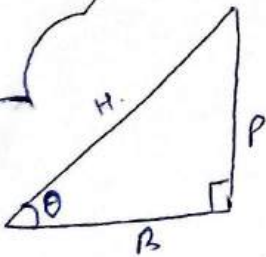
α

$$\phi = \frac{q}{2\epsilon_0} (1 - \cos\theta)$$

$\propto R^2$ if $\theta = 90^\circ$ [very-very large disc]

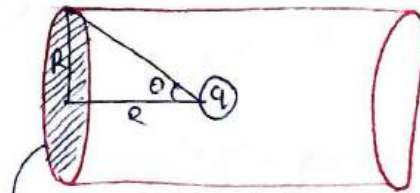
$$\phi_{disc} = \frac{q}{2\epsilon_0}$$

if $\theta = 0$ [very-small disc]
 $\phi = 0$



$$\sin\theta = \frac{P}{H} \quad ; \quad \tan\theta = \frac{P}{B}$$

$$\cos\theta = \frac{B}{H}$$



$$\phi_{(plate)} = \frac{q}{2\epsilon_0} (1 - \cos\theta)$$

$$\frac{q}{2\epsilon_0} \left(1 - \frac{1}{\sqrt{2}}\right)$$

$$\tan\theta = \frac{R}{R} = 1$$

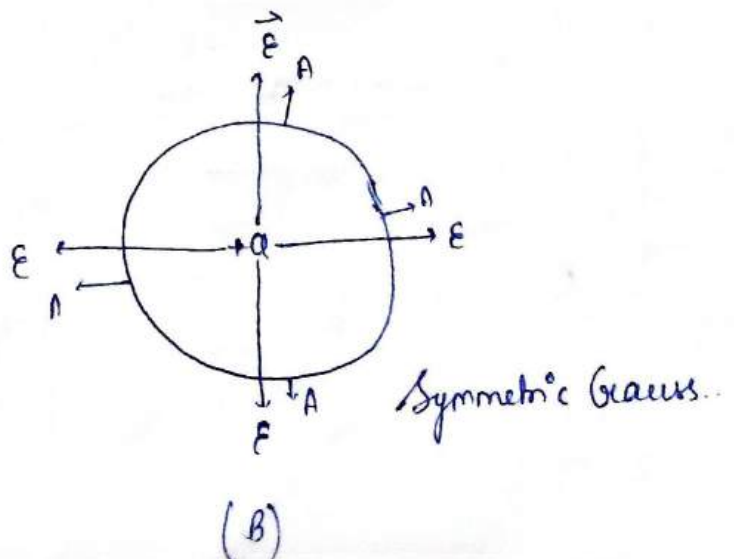
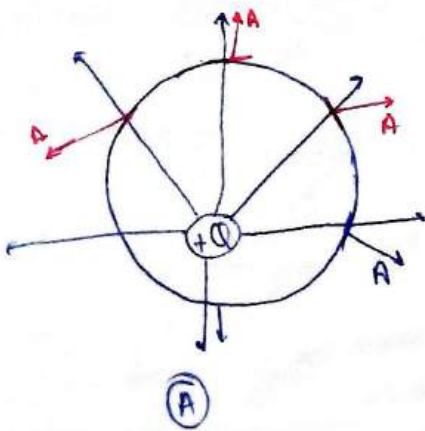
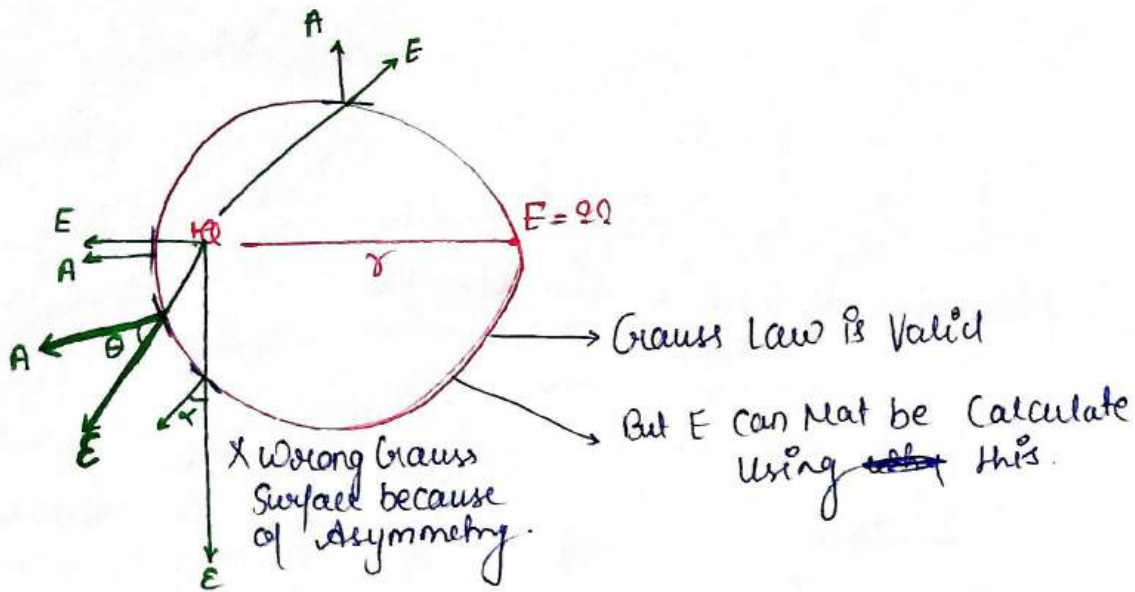
$$\theta = 45^\circ$$

Application of Gauss Law

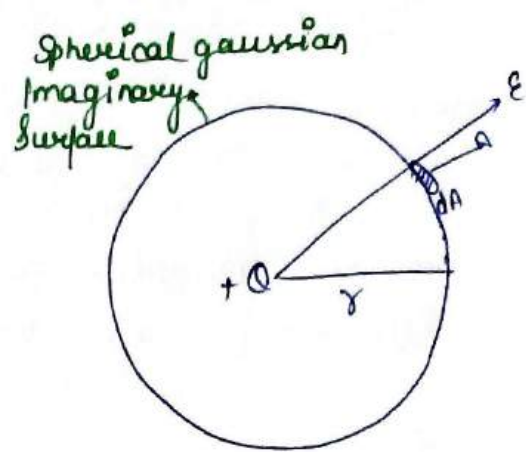
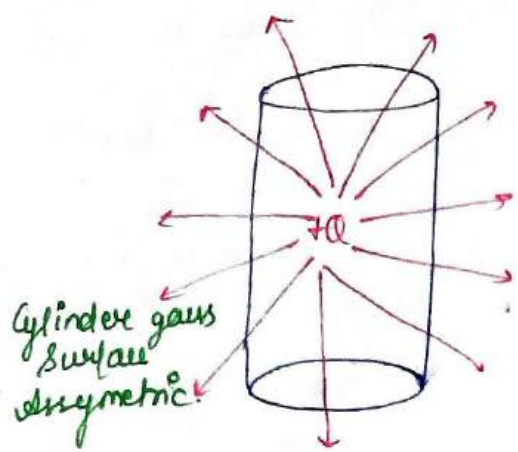
Step to Calculate electric field using Gauss Law

1. Draw clear symmetric gaussian surface.
2. Gaussian surface must be passing through the point where electric field have to be calculate.
3. Gauss surface must be symmetric to the charge distribution.
4. Angle b/w Gaussian surface and electric field must be $0^\circ, 90^\circ, 180^\circ$.
5. Apply $\oint \vec{E} \cdot d\vec{A} = \frac{q_{in}}{\epsilon_0}$.
6. Gauss law always Valid for every type of charge distribution but only useful to calculate electric field when charge distribution is symmetric..

(i) Electric field due to point charge using Gauss law.



(ii) Electric field due to Hollow non conducting sphere
Hollow / Solid conducting sphere / shell.



$$\oint \vec{E} \cdot d\vec{A} = \frac{q_{in}}{\epsilon_0}$$

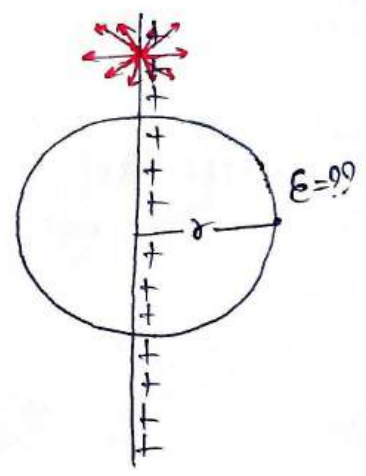
$$E \int dA \cos 0 = \frac{Q}{\epsilon_0}$$

$$E 4\pi r^2 = \frac{Q}{\epsilon_0}$$

$$E = \frac{Q}{4\pi \epsilon_0 r^2}$$

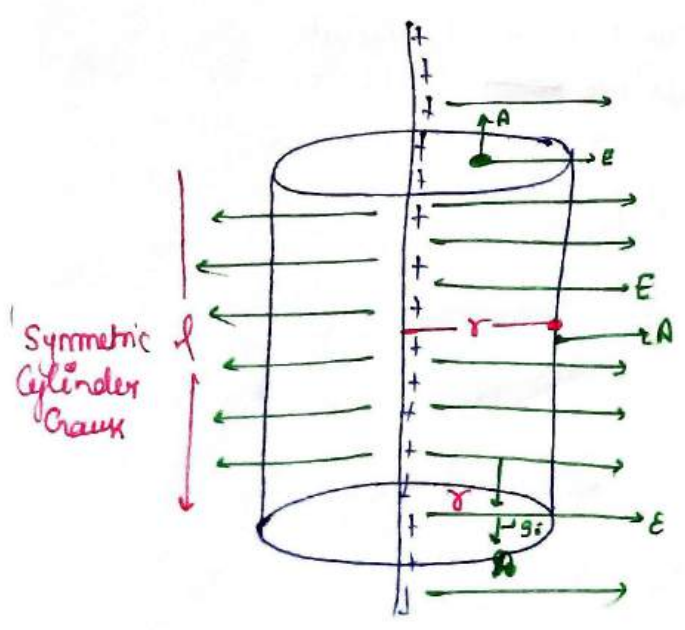
$$E = \frac{kQ}{r^2}$$

(iii) Electric field due to Infinite line charge



Conducting / metal / shell
Solid / hollow
always hollow sphere

(iv) Electric field due to Infinite line charge



$$\oint \vec{E} \cdot d\vec{A} = \frac{q_{in}}{\epsilon_0}$$

$$\oint E \cdot d\vec{A} \cos 90^\circ + \oint E dA \cos 0 + \oint E dA \cos 90^\circ$$

$$\oint E dA \cos 0 = \frac{q_{in}}{\epsilon_0}$$

$$E \int dA = \frac{q_{in}}{\epsilon_0}$$

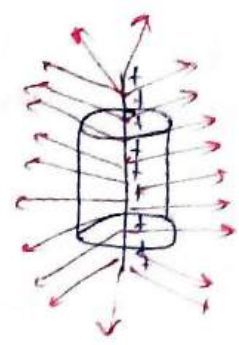
$$E \int dA = \frac{q_{in}}{\epsilon_0}$$

$$E \times 2\pi r L = \frac{\lambda L}{\epsilon_0}$$

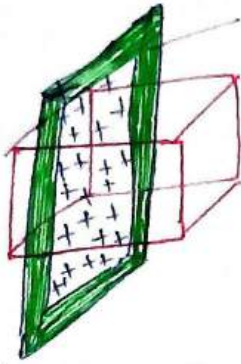
$$E = \frac{\lambda}{2\pi \epsilon_0 r} \times \frac{L}{L} \Rightarrow \sqrt{\frac{2\pi \lambda}{r} = E}$$

For finite line charge

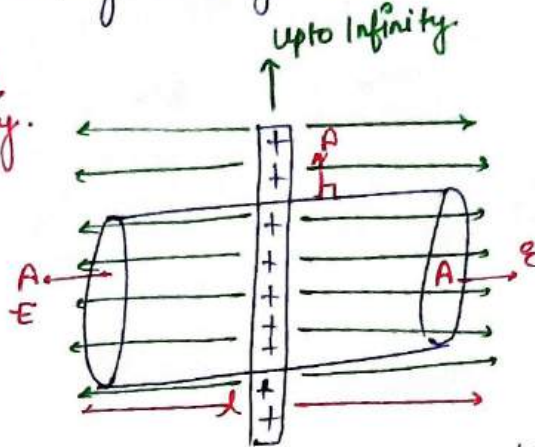
Gauss law is valid or not — Yes valid
But not useful to calculate electric field.



Infinity large non conducting charge sheet



$\sigma =$ Surface charge density.



$$\oint \vec{E} \cdot d\vec{A} \cos 0 + \int \vec{E} \cdot d\vec{A} \cos 90 + \int \vec{E} \cdot d\vec{A} \cos 0 = \frac{q_{in}}{\epsilon_0}$$

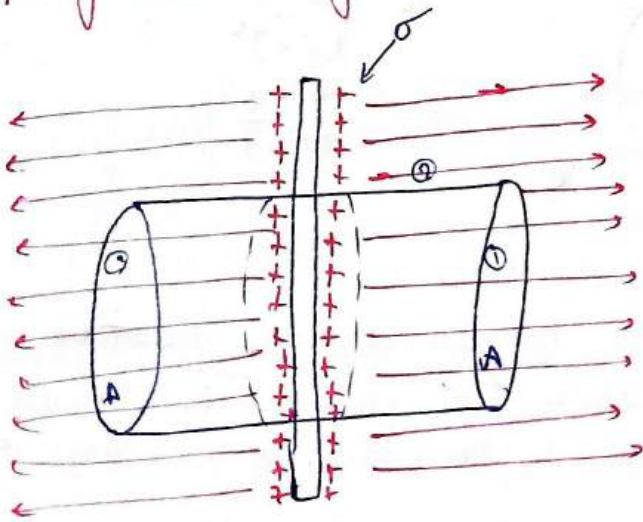
$$2E \phi dA = \frac{q_{in}}{\epsilon_0}$$

$$2EA = \frac{\sigma A}{\epsilon_0}$$

$$E = \frac{\sigma}{2\epsilon_0}$$

Uniform

Infinity Conducting sheet



$$\phi_1 + \phi_2 + \phi_3 = \frac{q_{in}}{\epsilon_0}$$

$$2 \int \vec{E} \cdot d\vec{A} = \frac{q_{in}}{\epsilon_0}$$

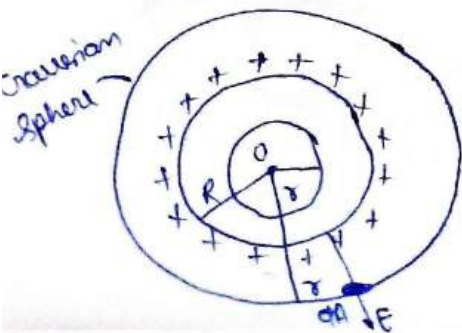
$$2E \phi dA = \frac{\sigma dA}{\epsilon_0}$$

$$EA = \frac{\sigma A}{\epsilon_0}$$

$$E = \frac{\sigma}{\epsilon_0}$$

Conducting Sheet

Electric field due to Hollow / Solid conducting sphere and nonconducting hollow sphere.



Inside ($r < R$)

$$E_{in} = 0$$

$$E_{centre} = 0$$

$$E_{surface} = \frac{kQ}{R^2}$$

$$E_{out} = \frac{kQ}{r^2}$$

Outside ($r > R$)

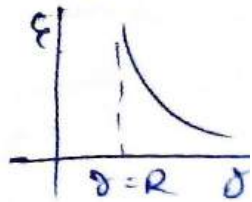
$$\oint \vec{E} \cdot d\vec{A} = \frac{q_{in}}{\epsilon_0}$$

$$E \times 4\pi r^2 = \frac{Q}{\epsilon_0}$$

$$E = \frac{kQ}{r^2}$$

Same as point charge

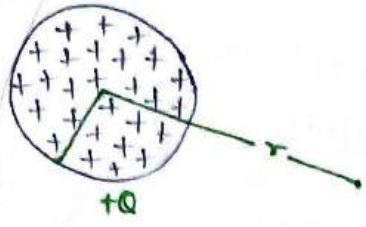
Electric field and distance



Electric field inside non conducting solid sphere / Charge uniformly distributed inside sphere

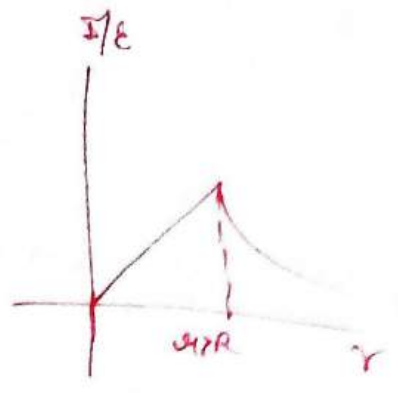
$$I_{\text{solid (outside)}} = \frac{QM}{r^2}, \quad I_{\text{surf}} = \frac{QM}{R^2}, \quad I_{\text{in}} = \frac{QM r}{R^3}$$

$$E_{\text{out}} = \frac{kQ}{r^2}, \quad E_{\text{surf}} = \frac{kQ}{R^2}, \quad E_{\text{in}} = \frac{kQ r}{R^3}$$



$$E_{\text{in}} = \frac{\rho \cdot 4\pi r^3}{3 \cdot 4\pi r^2 \epsilon_0}$$

$$E_{\text{in}} = \frac{\rho r}{3\epsilon_0}$$

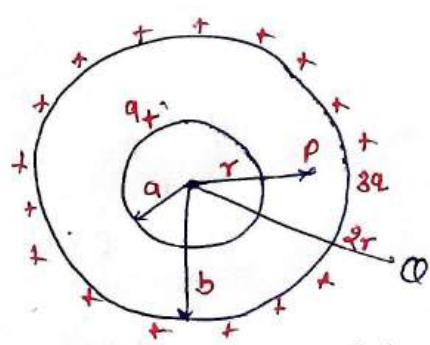


Volume charge density

$$\rho = \frac{Q}{\frac{4}{3}\pi R^3}, \quad \frac{Q}{R^3} = \frac{4}{3}\pi\rho$$

Ques The electric field intensity at P and Q in the shown arrangement are in the ratio.

- ① 1:2
- ② 2:1
- ③ 1:1 ✓
- ④ 4:3



$$E_p = \frac{kq}{r^2}$$

$$E_q = \frac{4kq}{(2r)^2}$$

$$\frac{4kq}{4r^2}$$

Hollow concentric shell

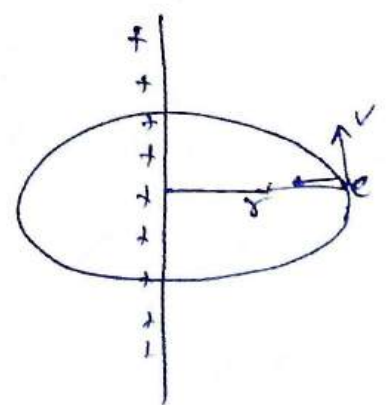
Ques An electron is rotating around an infinite positive linear charge in a circle of radius 0.1m if the linear charge density is $1 \mu\text{e}/\text{cm}$. Then the velocity of electron in m/s will be.

- 1. 0.562×10^7
- 2. 5.62×10^7
- 3. 562×10^7
- 4. 0.0562×10^7

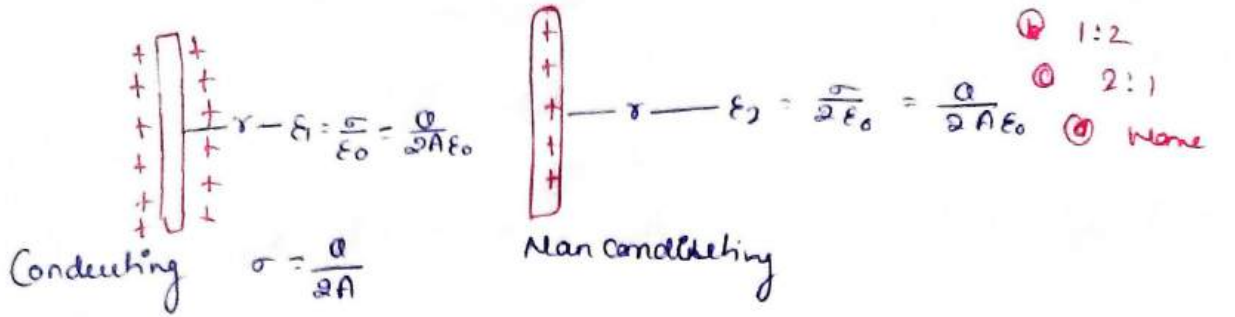
$$\frac{mv^2}{r} = qE$$

$$\frac{mv^2}{r} = e \left(\frac{2k\lambda}{r} \right)$$

$$v = \sqrt{\frac{2k\lambda e}{m}}$$

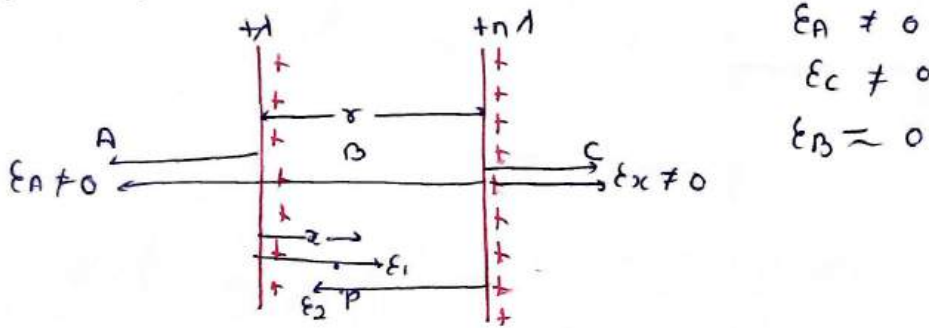


Q1 Charge Q is given to conducting and non conducting large sheet respectively then find Ratio of electric field near surface of plate



- Ⓐ 1:1
- Ⓑ 1:2
- Ⓒ 2:1
- Ⓓ None

Q2 Find position where electric field will be zero. due to infinite charge



$$E_P = 0$$

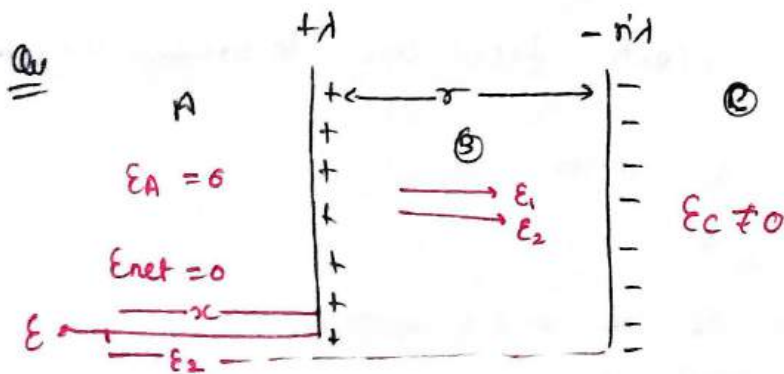
$$E_1 = E_2$$

$$\frac{2k\lambda}{x} = \frac{2kn\lambda}{r-x}$$

$$nx = r-x$$

$$nx + x = r$$

$$x = \left(\frac{r}{n+1}\right)$$



Q3 Then find position where electric field is zero.

$$E_1 = E_2$$

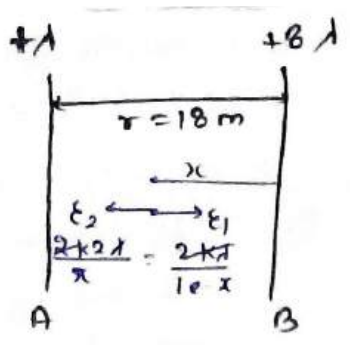
$$\frac{2k\lambda}{x} = \frac{2kn\lambda}{r+x}$$

$$nx - x = r$$

$$x = \left(\frac{r}{n-1}\right)$$

from +d charge

Ques



$$18 \times 8 - 8x = x$$

$$144 - 8x = x$$

$$144 = 9x$$

$$x = 16$$

Find distⁿ from B where electric field is zero.

3rd method

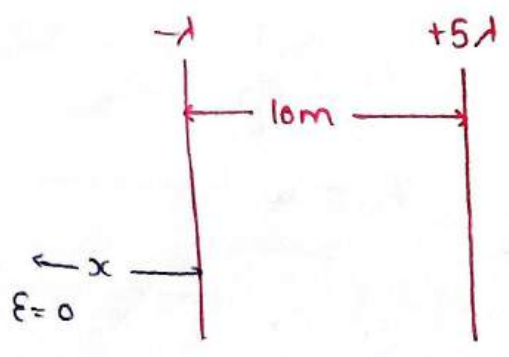
$$x = \frac{18}{8+1}$$

$$x = \frac{18 \times 2}{9}$$

from +8 \rightarrow = $18 - 2 = 16m$

Ques

Find position where electric field is zero



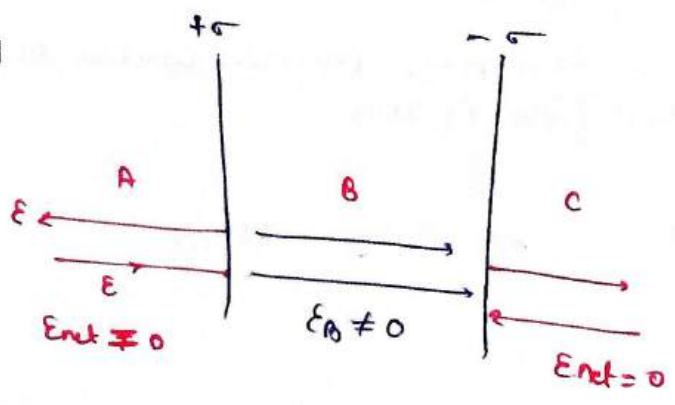
$$x = \frac{10}{5-1} = \frac{10}{4} = 2.5m$$

(from -1)

from (+5) = $y = 12.5$

Electric field due to combination of sheet :-

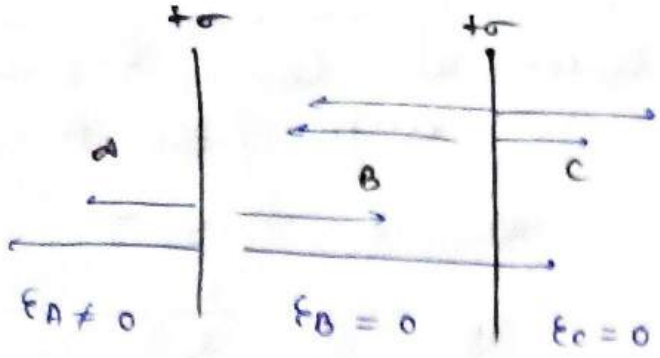
Ques



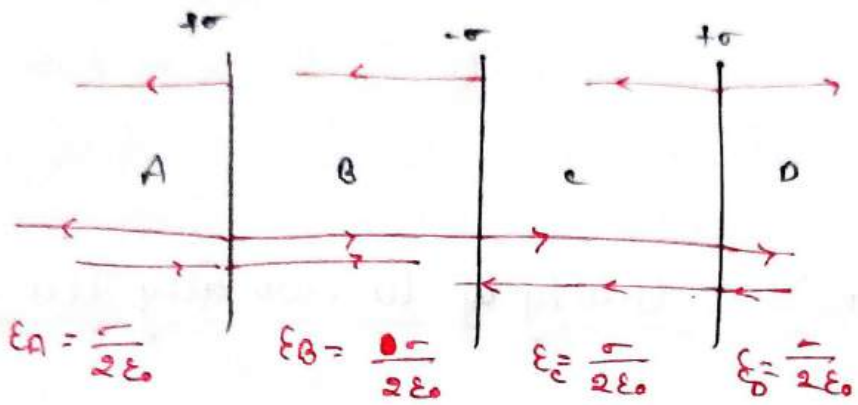
Electric field zero in which region

- ① In A
- ② In B
- ③ In A & C
- ④ Not any region

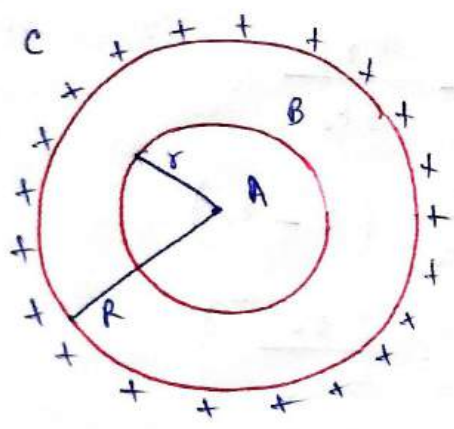
Ques



Sheet

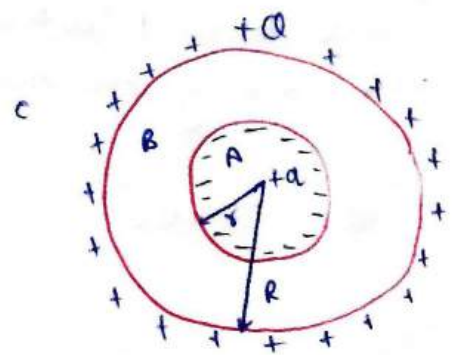


Electric field due to thick sphere (conducting sphere)



$E_A = 0$
 $E_B = 0$
 $E_C \neq 0$

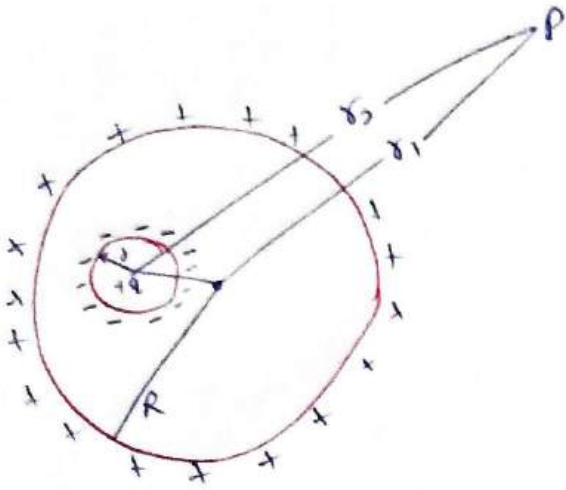
Electric field due to thick conducting sphere having charge q at centre of cavity & Q at surface of sphere.



$E_A \neq 0$
 $E_B = 0$ (inside conductor always zero)
 $E_C \neq 0$

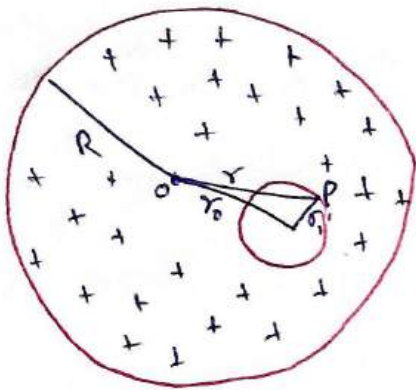
$E_C = \frac{k(Q+q)}{r^2}$

Ques Conducting Neutral Solid Sphere having Cavity and q is placed at centre of cavity find electric field at 'P'



- (a) $E = \frac{kq}{r_1^2}$ ✓
 (b) $E = \frac{kq}{r_2^2}$
 (c) $E = \frac{kq}{(r_1 - r_2)^2}$
 (d) None of these

Electric field Inside Cavity of Uniformly charge Solid Sphere



$$\vec{E}_0 + \vec{E}_1 = \vec{E}_2$$

$$\vec{E} = (\text{E}_{\text{comp. sp.}})_P - (\text{E}_{\text{cavity}})_P$$

due to remaining

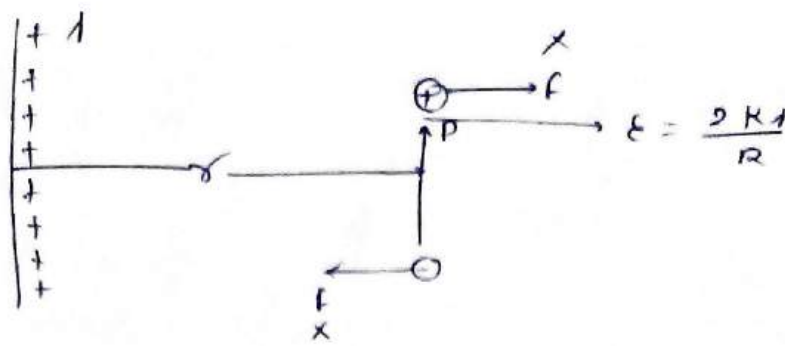
$$\frac{\rho r_1^3}{3\epsilon_0} = \frac{\rho r_2^3}{3\epsilon_0}$$

$$= \frac{\rho}{3\epsilon_0} (r_1^3 - r_2^3)$$

Uniform field. $E_{\text{cavity}} = \frac{\rho r_0}{3\epsilon_0}$

Ques A dipole with an electric moment \vec{p} is located at a distance r from a long thread charged uniformly with a linear charge density λ . Find the force F acting on the dipole if the vector \vec{p} is oriented along the thread

- (1) $\frac{p\lambda}{2\pi\epsilon_0 r^2}$ (2) $\frac{p\lambda}{2\pi\epsilon_0 r}$ (3) $\frac{p}{2\pi\epsilon_0 \lambda}$ (4) zero



Q11

Q11 If a small sphere

- ① $\epsilon_0 \left(\frac{mg}{a} \right) \tan \theta$
- ② $\epsilon_0 \left(\frac{2mg}{a} \right) \tan \theta$
- ③ $\epsilon_0 (mgq) \tan \theta$
- ④ $\epsilon_0 \left(\frac{mg}{3q} \right) \tan \theta$

Q11 Two long thin

1. $\frac{kqA}{d}$

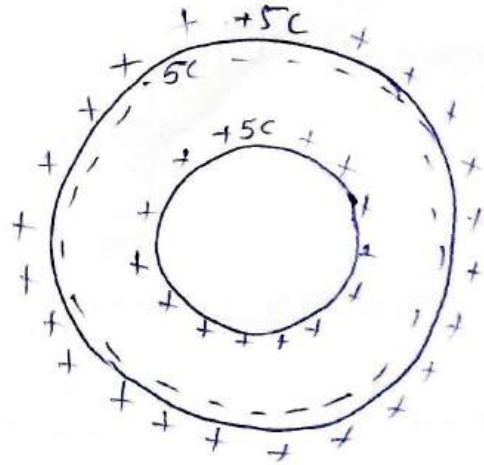
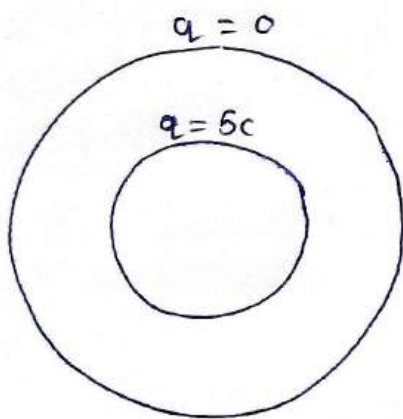
2. $\frac{kqA^2}{d}$ ✓

3. $\frac{kqA}{d^2}$

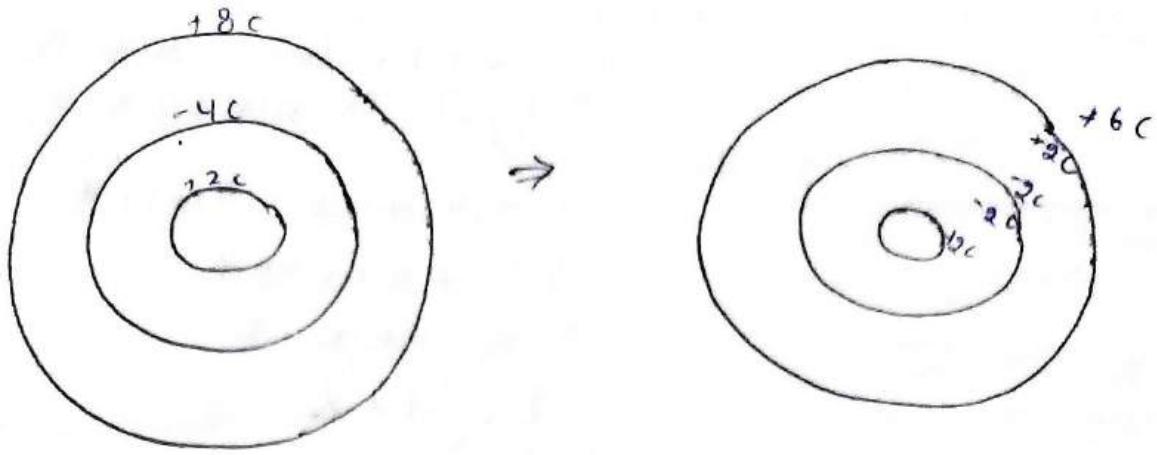
4. $\frac{kqA^2}{d^2}$

~~Q12~~ Charge distribution on Concentric sphere.

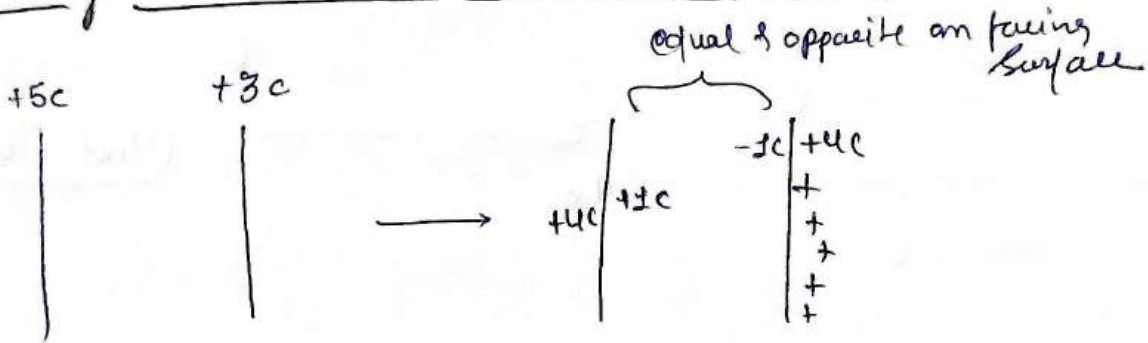
Find charge on inner & outer surface of both the sphere



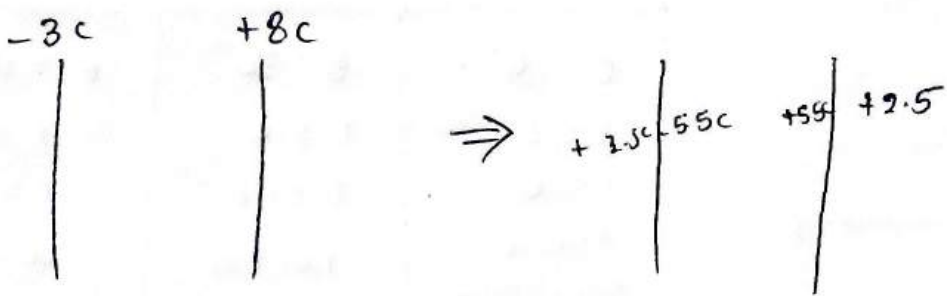
Q1



Charge distribution on Conductor parallel sheet.



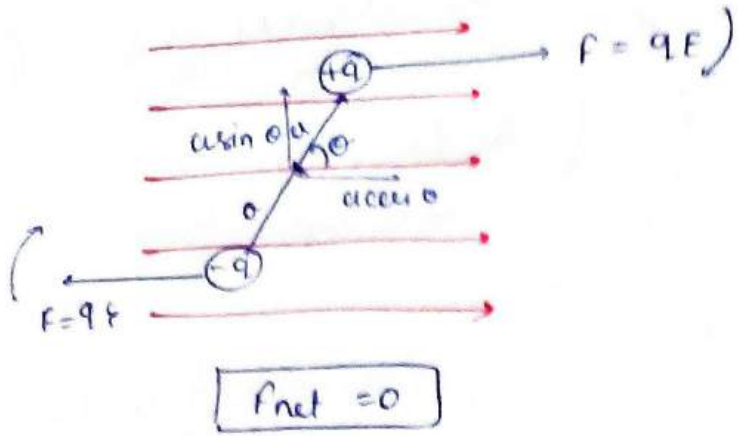
Q2



Charge on outer surface of plate = $\frac{Q_{total}}{2}$

Electric dipole in uniform electric field

electrostatic force on dipole is always zero.



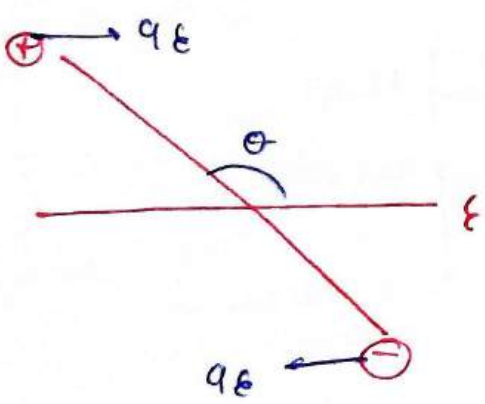
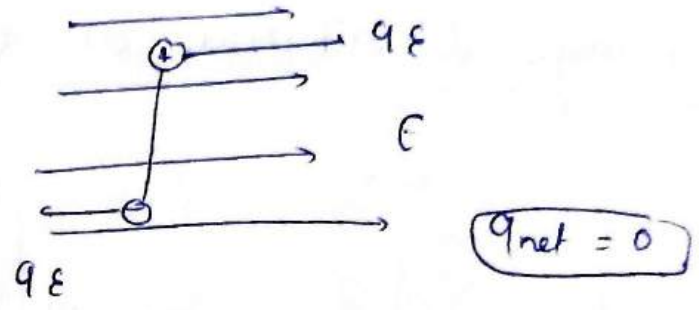
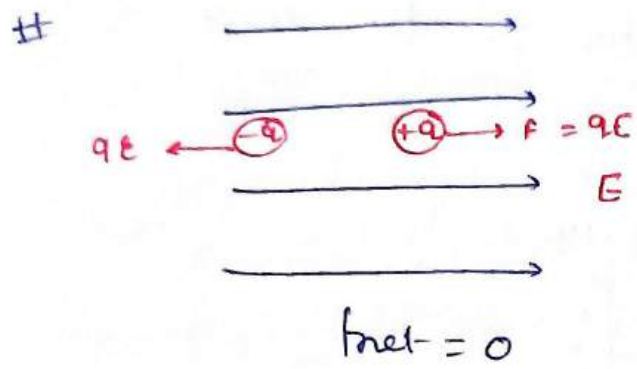
$$\tau = qE a \sin \theta + qE a \sin \theta$$

$$\tau = 2qE a \sin \theta$$

$$\tau = pE \sin \theta$$

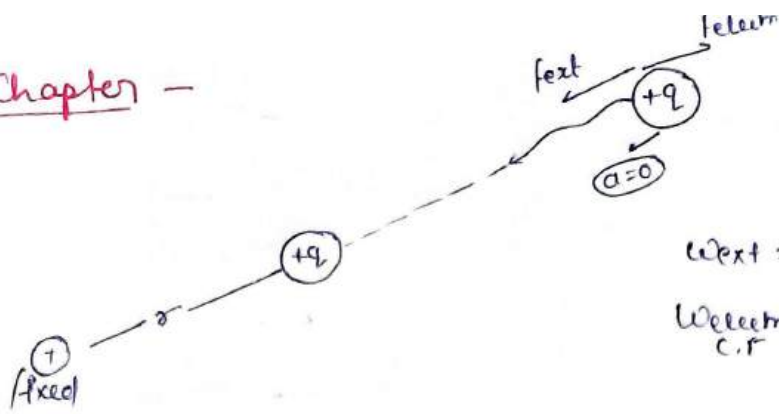
$$\vec{\tau} = \vec{p} \times \vec{E}$$

$$\tau = pE \sin \theta$$



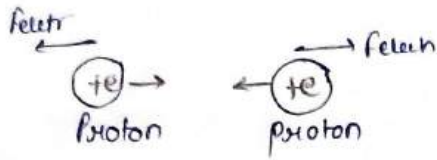
$\theta = 0^\circ$	$\theta = 90^\circ$	$\theta = 180^\circ$
$F = 0$	$F = 0$	$F = 0$
$\tau = 0$	$\tau = pE$	$\tau = 0$
stable equilibrium	not stable equilibrium	unstable equilibrium

Last Chapter -



$W_{ext} = +ve$
 $W_{electr} = -ve = \Delta U$
 c.r

Ques



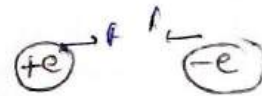
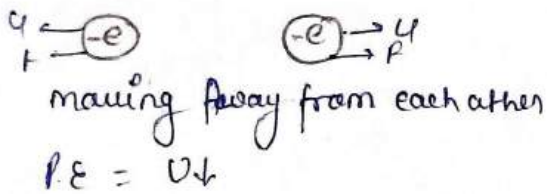
$U(\text{potential}) = U \uparrow$

Ex!

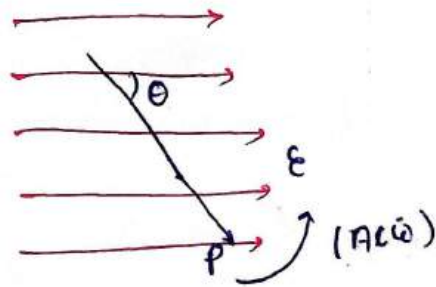
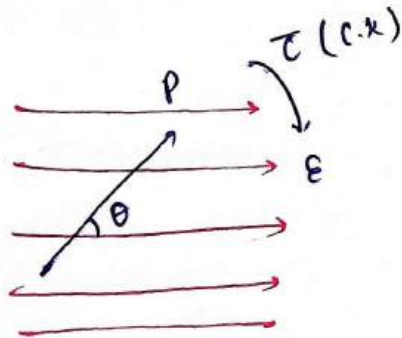


$P.E = U \uparrow$

Ques



$P.E = U \downarrow$

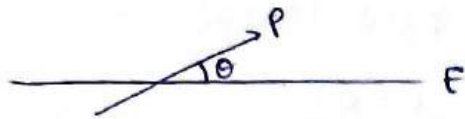


$\tau = PE \sin \theta$

$\theta = 0^\circ$	$\theta = 90^\circ$	$\theta = 180^\circ$
$f = 0$	$f = 0$	$f = 0$
$\tau = 0$	$\tau_{max} = PE$	
Stable equilibrium		Unstable equilibrium.

dipole in uniform electric field always in translational equilibrium - True.

Oscillation of dipole in uniform electric field



$$\tau = PE \sin \theta$$

$$I \alpha = PE \sin \theta$$

S.H.M θ (small)

$$\alpha = \left(\frac{PE}{I} \right) \theta$$

$$\vec{\alpha} = \left(\frac{PE}{I} \right) \vec{\theta}$$

$$\omega^2 = \frac{PE}{I}$$

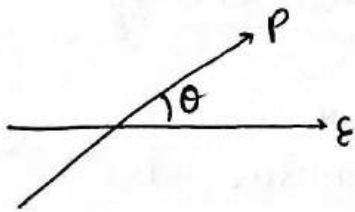
$$\omega = \sqrt{\frac{PE}{I}}$$

$$T = 2\pi \sqrt{\frac{I = m r^2}{PE = m \omega^2 r^2}}$$

$$T = 2\pi \sqrt{\frac{I}{P \cdot E}}$$

I = moment of inertia
 P = dipole moment
 E = Electric field.

Ques



find taken by dipole to come in the direction of electric.

① $T = 2\pi \sqrt{\frac{I}{P \cdot E}}$

② $T = \pi \sqrt{\frac{I}{P \cdot E}}$

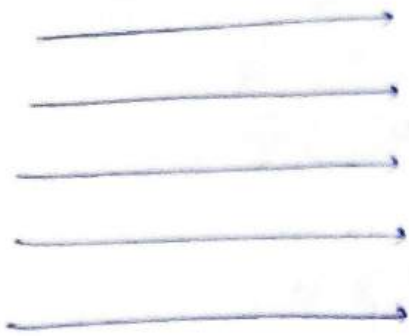
③ $T = \frac{\pi}{2} \sqrt{\frac{I}{P \cdot E}}$ ✓

Compare dimension / unit of energy & torque.

$$\text{Energy} = f \times \text{dist}^n = J = \text{Nm} = \text{ML}^2\text{T}^{-2}$$

$$\text{torque} = \vec{C} = \vec{r} \times \vec{F} = \text{Nm} = \text{ML}^2\text{T}^{-2}$$

Electrostatic potential energy stored in dipole in electric field.



$$\Delta u = -W_{e,f}$$

$$du = -(\vec{c} \cdot d\vec{\theta})$$

$$du = -\tau d\theta \cos 180^\circ$$

$$du = +\tau d\theta$$

$$\int_{90}^{\theta} du = PE \int_{90}^{\theta} \sin \theta d\theta$$

$$U_{\theta} - U_{90} = PE (\cos \theta)_{90}^{\theta}$$

$$U_{\theta} = -PE (\cos \theta - \cancel{\cos 90})$$

$$U = -PE \cos \theta$$

$$\boxed{U = -\vec{p} \cdot \vec{E}}$$

Torque

- Vector
- dimension $-ML^2T^{-2}$
- unit - Nm

$$\vec{c} = \vec{p} \times \vec{E}$$

$$PE \sin \theta$$

Torque on dipole in electric field

Potential energy

- Scalar
- Dimension $-ML^2T^{-2}$
- Unit - Nm

$$\boxed{U = -\vec{p} \cdot \vec{E}}$$

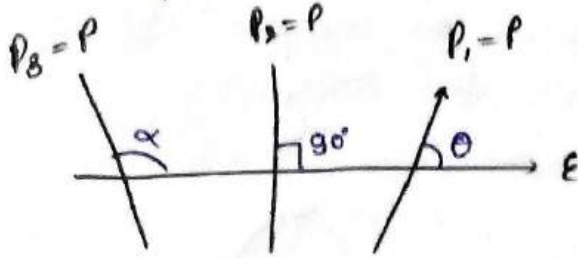
$$= -PE \cos \theta$$

dipole store energy in (E)

$\theta = 0^\circ$	$\theta = 90^\circ$	$\theta = 180^\circ$
$F = 0$	$F = 0$	$F = 0$
$\tau = 0$	$\tau = PE$	$\tau = 0$
$U = -PE$	$U = 0$	$U = -PE \cos 180$

Increasing Order of P.E

Ques



$$U_3 > U_2 > U_1$$

$$U = -PE \cos \theta$$

$$W_{ext} = \Delta U$$

$$W_{c.f} = -\Delta U$$

Ques Find work done to rotate the dipole from stable to unstable equilibrium??

- ① PE
 ② 2PE ✓
 ③ -2PE
 ④ -PE

$$W_{c.f} = -\Delta U$$

$$W_{ext} = \Delta U$$

$$W_{ext} = U_f - U_i$$

$$PE = (-PE)$$

$$2PE$$

Ques Find work done to rotate from stable to unstable equilibrium by electric field.

$$W_{c.f} = -\Delta U$$

$$W_{ext} = -2PE$$

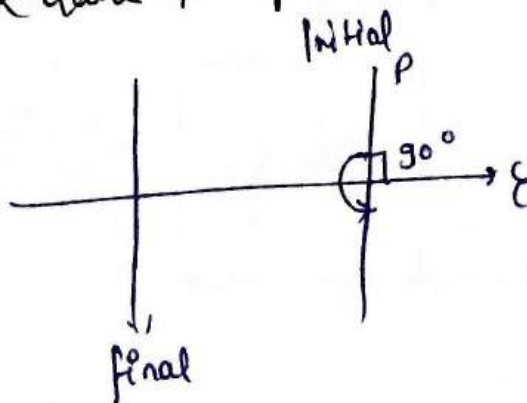
$$-(U_f - U_i)$$

$$U_i - U_f$$

$$-PE - PE = -2PE$$

Ques Find work done to dipole as shown in fig from initial to final

- ① PE
 ② $\frac{PE}{2}$
 ③ 2PE
 ④ zero ✓



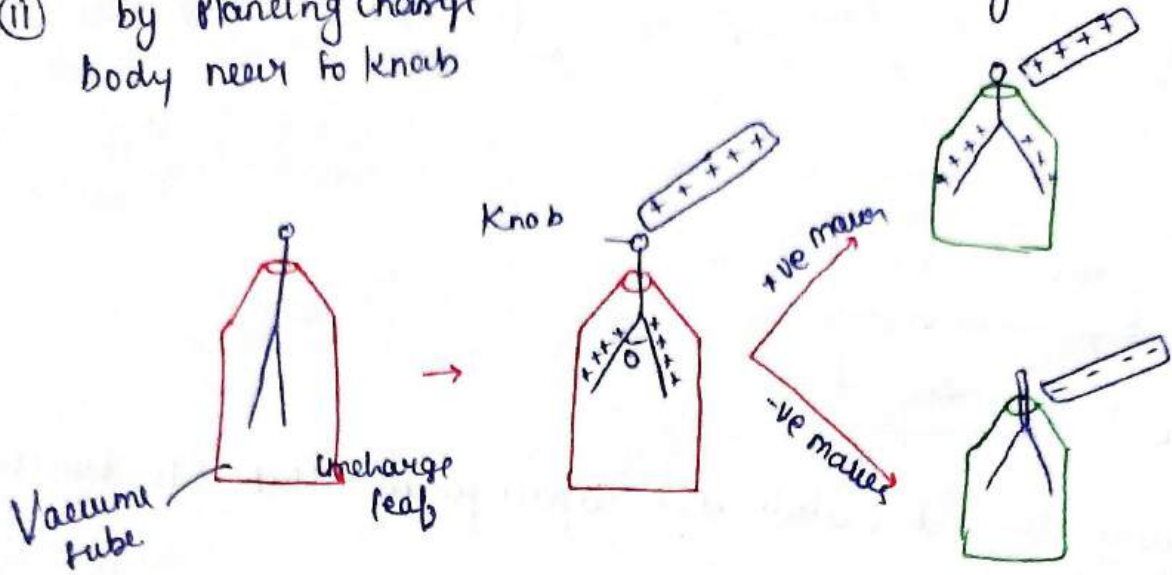
$$U_i = 0$$

$$U_f = 0$$

$$W = \Delta U = 0$$

Gold leaf electroscope → Is an instrument use to detect or compare charge on the body

- (i) by touching
- (ii) by placing charge body near to knob



Ques when a $+20\text{ C}$ rod is touched to the knob the deflection of leaves was 5° and when an identical rod of -40 C is touched the deflection was found to be 9° . if an identical rod of $+30$ is touched then the deflection may be.

- (a) 0
 - (b) 2°
 - (c) 7° ✓
 - (d) 11°
- $\theta \propto \text{charge}$
- | | | |
|----------------|---|-----------|
| 20 C | → | 5° |
| -40 C | → | 9° |

Ques A glass rod rubbed with silk is touched with the disc of negatively charged gold leaf electroscope then divergence

